

# Machine learning from precision medicine

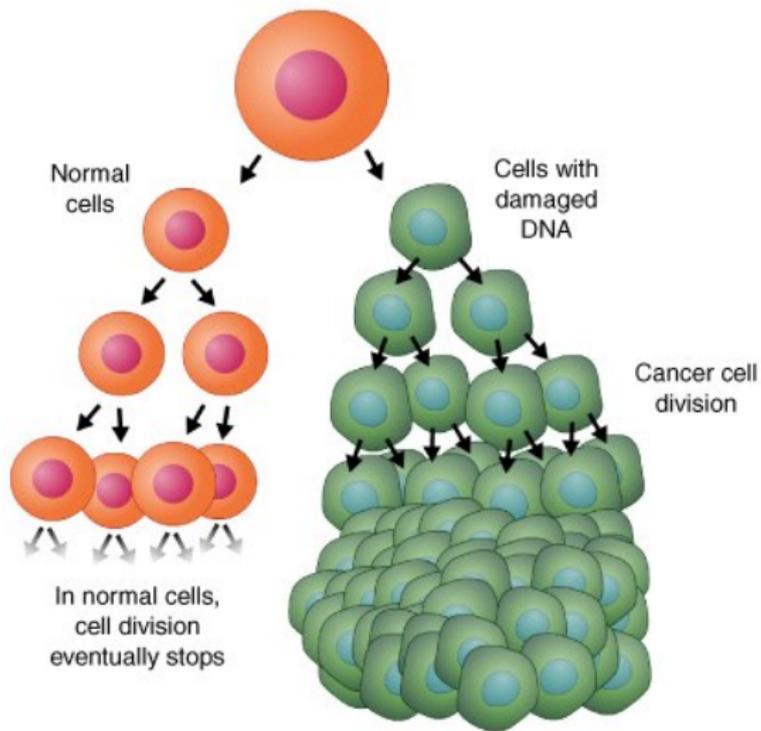
Jean-Philippe Vert

jean-philippe.vert@ens.fr

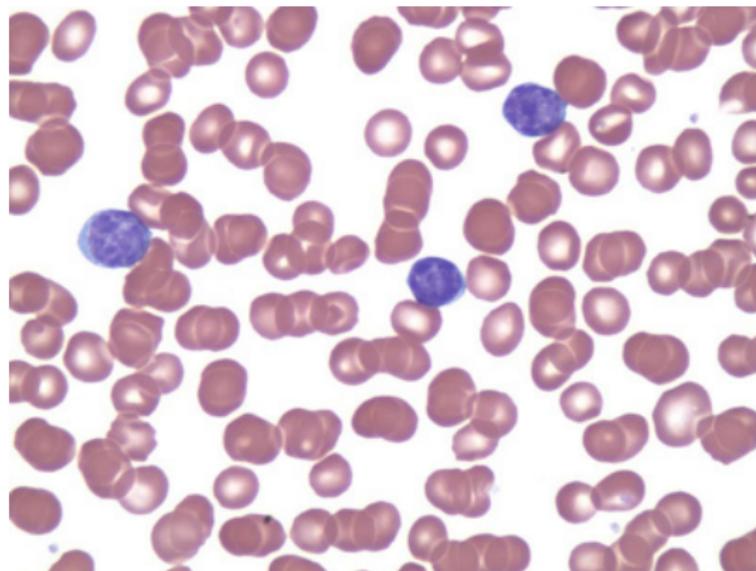


Krupp Symposium "From Machine Learning to Personalize  
Medicine", Munich, October 21, 2016

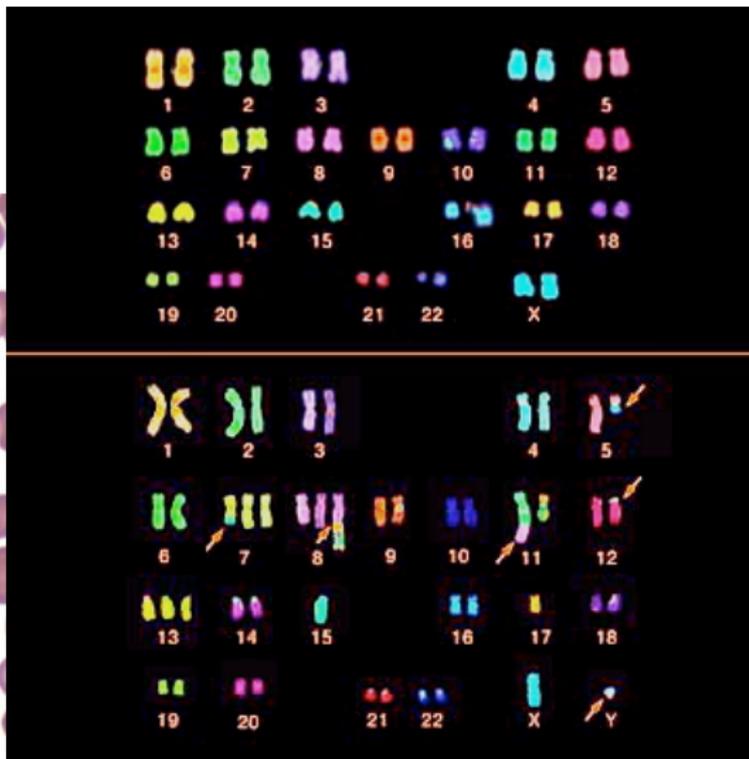
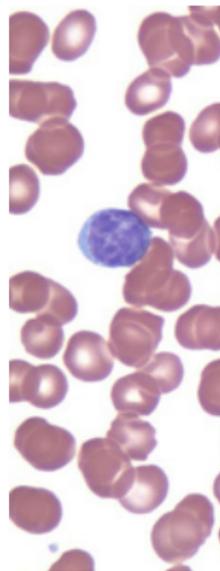
# Cancer



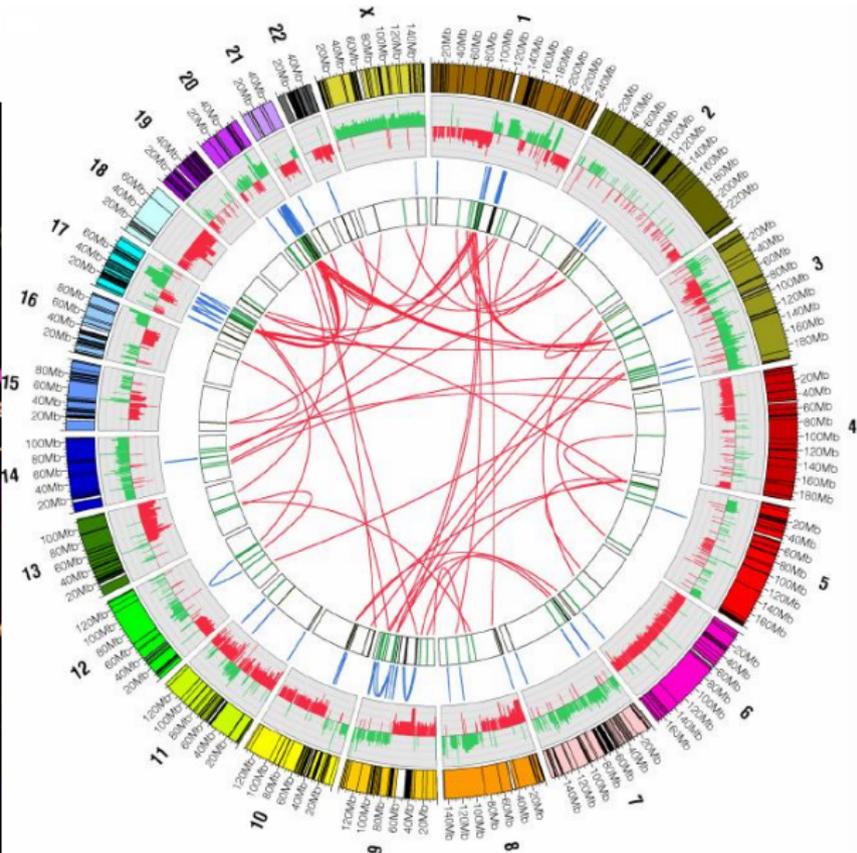
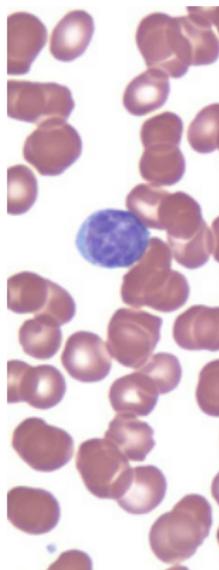
## A cancer cell (1900)



# A cancer cell (1960)

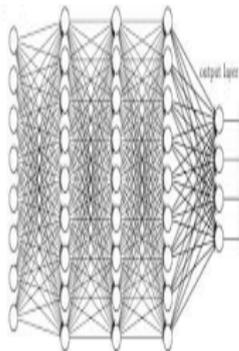
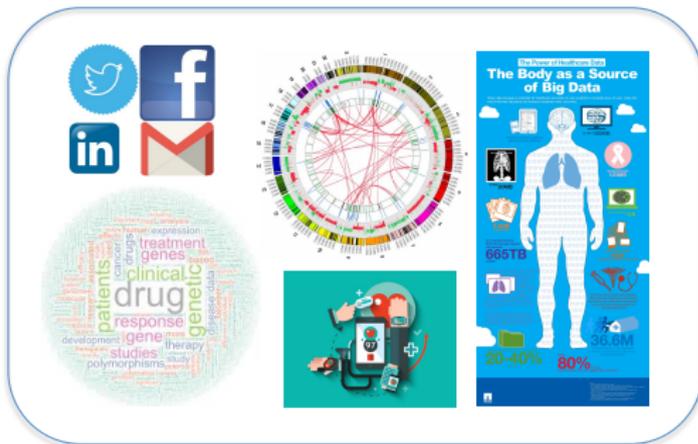


# A cancer cell (2010)





# Opportunities



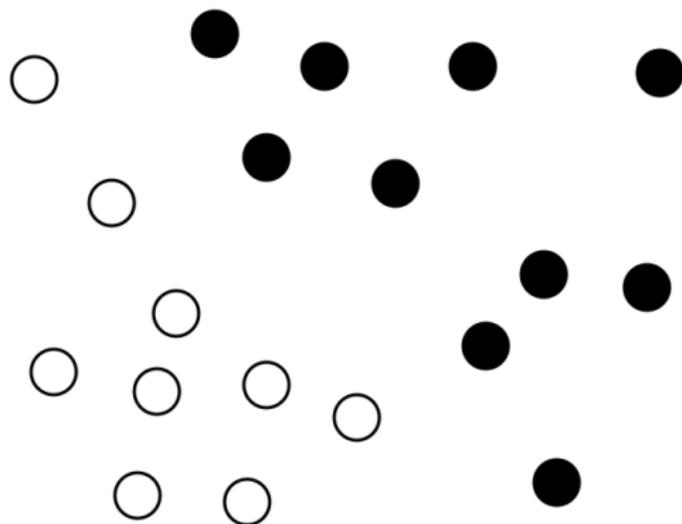
- What is your risk of developing a cancer? (*prevention*)
- Once detected, what precisely is your cancer? (*diagnosis*)
- After treatment, are you cured? (*prognosis*)
- What is the best way to treat your cancer? (*precision medicine*)

# Example: precision medicine



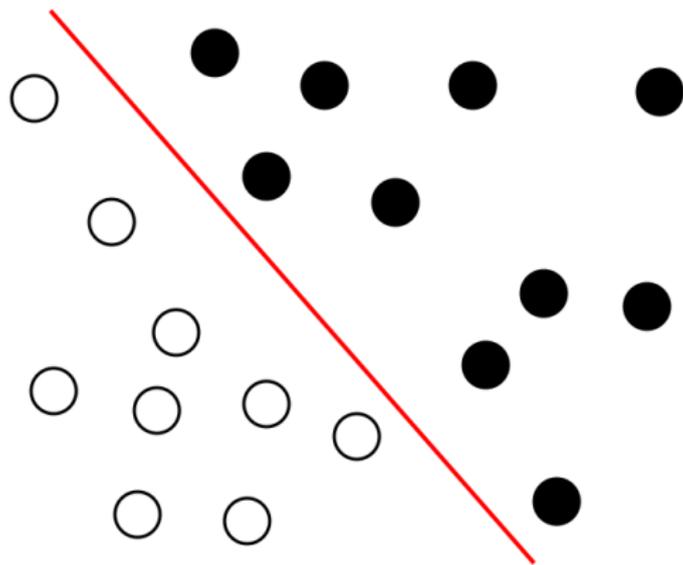
# Learning from data (EASY case)

- Good vs Bad responders
- $n(= 19)$  patients  $\gg$   $p(= 2)$  genes



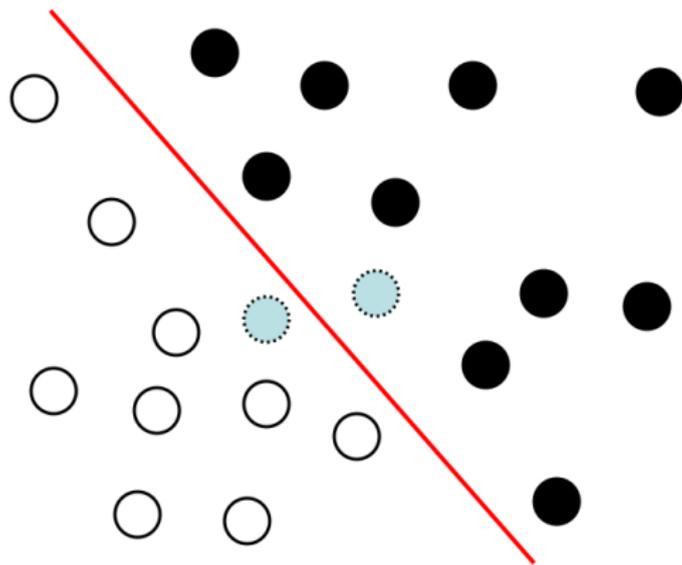
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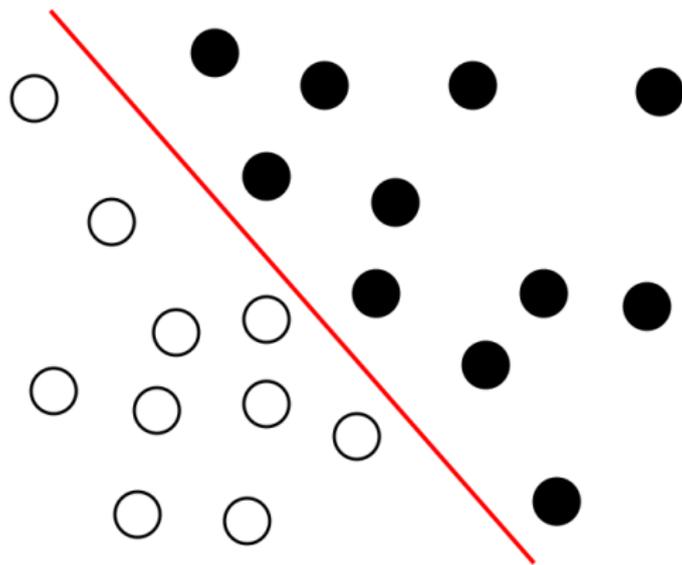
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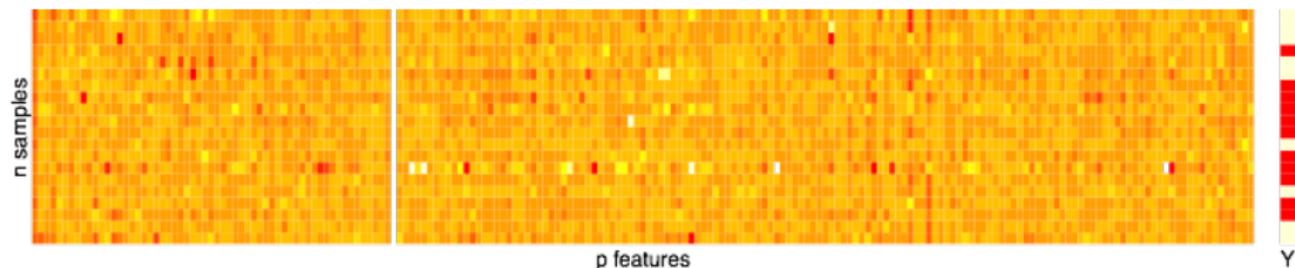


# Learning from data (EASY case)

- Good vs Bad responders
- $n(= 19)$  patients  $\gg$   $p(= 2)$  genes



## \*-omics challenge: $n \ll p$



- $n = 10^2 \sim 10^4$  (patients)
- $p = 10^4 \sim 10^7$  (genes, mutations, copy number, ...)
- Data of **various nature** (continuous, discrete, structured, ...)
- Data of **variable quality** (technical/batch variations, noise, ...)

### Consequences:

- Accuracy drops
- Biomarker selection unstable
- Speed and scalability can become an issue

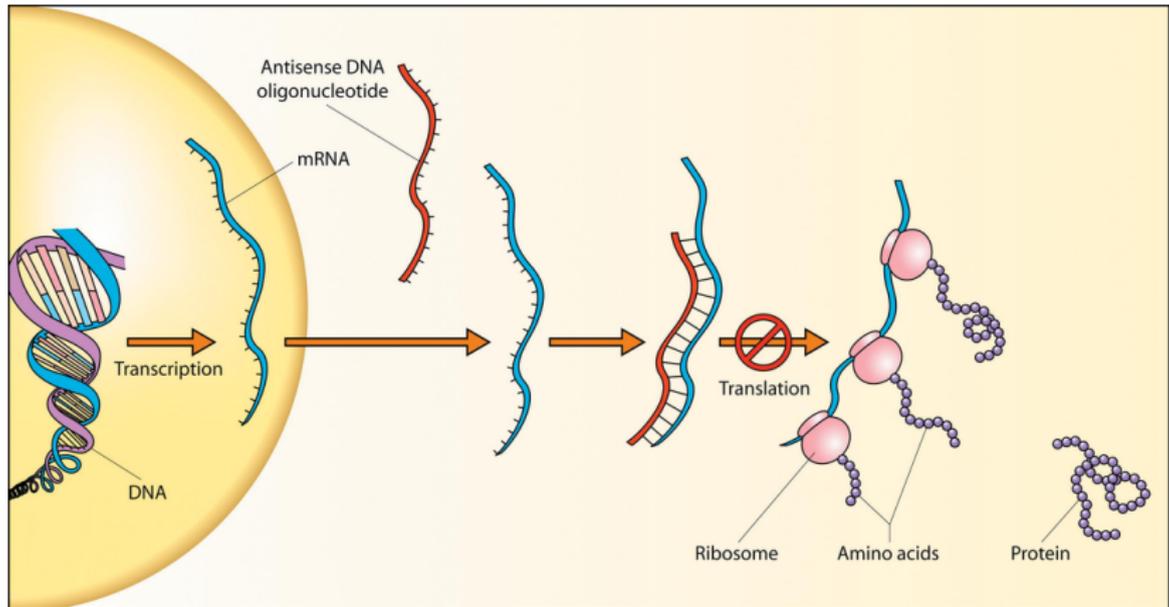
# Outline

- 1 Learning from gene expression data
- 2 Learning from mutation data
- 3 Conclusion

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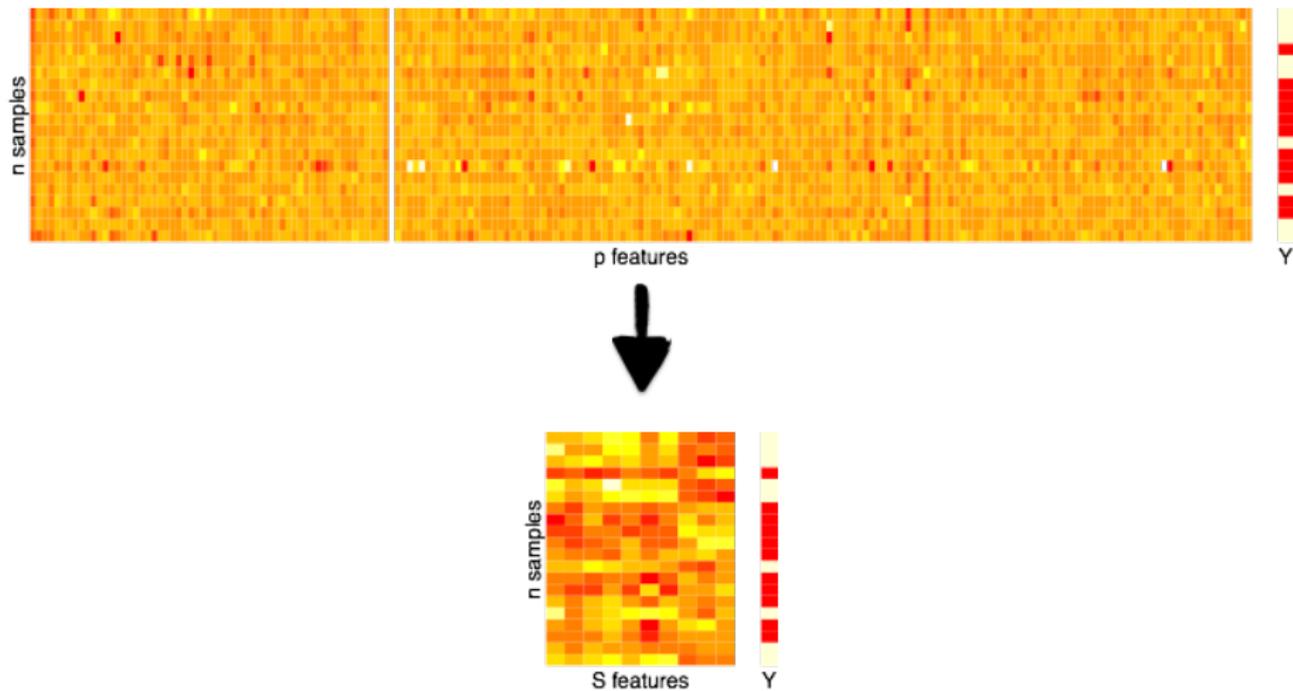
# Gene expression



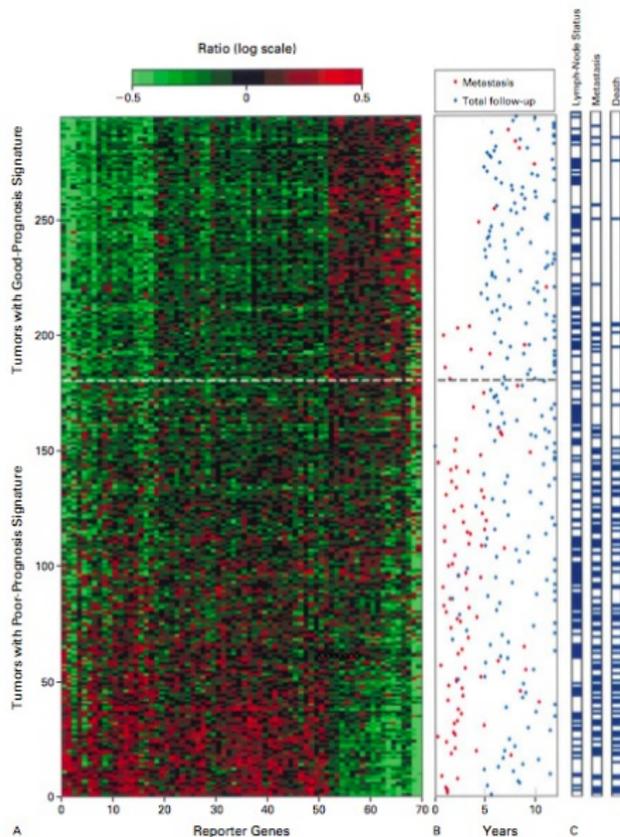
<http://mrsbabbkv.weebly.com/rna--protein.html>

- About 22,000 genes encoded in DNA (same for all cells)
- Expression of each gene (= RNA synthesis) varies between cells
- Can be measured for all genes simultaneously with sequencing

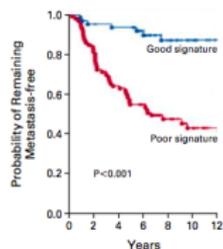
# Feature selection (a.k.a. *molecular signature*)



# Example: 70-gene breast cancer prognostic signature



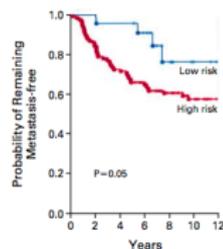
**A Gene-Expression Profiling**



No. At Risk

Good signature 60 57 54 45 31 22 12  
Poor signature 91 72 55 41 26 17 9

**B St. Gallen Criteria**



No. At Risk

Low risk 22 22 21 17 9 5 2  
High risk 129 107 88 69 48 34 19



van 't Veer et al. (2002);  
van de Vijver et al. (2002)

# But...

## Gene expression profiling predicts clinical outcome of breast cancer

Laura J. van 't Veer\*†, Hongyue Dai†‡, Marc J. van de Vijver\*†, Yudong D. He‡, Augustinus A. M. Hart\*, Mao Mao‡, Hans L. Peterse\*, Karin van der Kooy\*, Matthew J. Marton‡, Anke T. Witteveen\*, George J. Schreiber‡, Ron M. Kerkhoven\*, Chris Roberts‡, Peter S. Linsley‡, René Bernards\* & Stephen H. Friend‡

\* Divisions of Diagnostic Oncology, Radiotherapy and Molecular Carcinogenesis and Center for Biomedical Genetics, The Netherlands Cancer Institute, 121 Plesmanlaan, 1066 CX Amsterdam, The Netherlands  
‡ Rosetta Inpharmatics, 12040 115th Avenue NE, Kirkland, Washington 98034.

70 genes (Nature, 2002)

## Gene-expression profiles to predict distant metastasis of lymph-node-negative primary breast cancer

Yixin Wang, Jan G M Kljin, Yi Zhang, Anieta M Sieuwerts, Maxime P Look, Fei Yang, Dmitri Talantov, Mieke Timmermans, Marion E Meijer-van Gelder, Jack Yu, Tim Jatko, Els M J J Berns, David Atkins, John A Foekens

76 genes (Lancet, 2005)

3 genes in common

van 't Veer et al. (2002); Wang et al. (2005)

# 3 genes is the best you can expect given $n$ and $p$

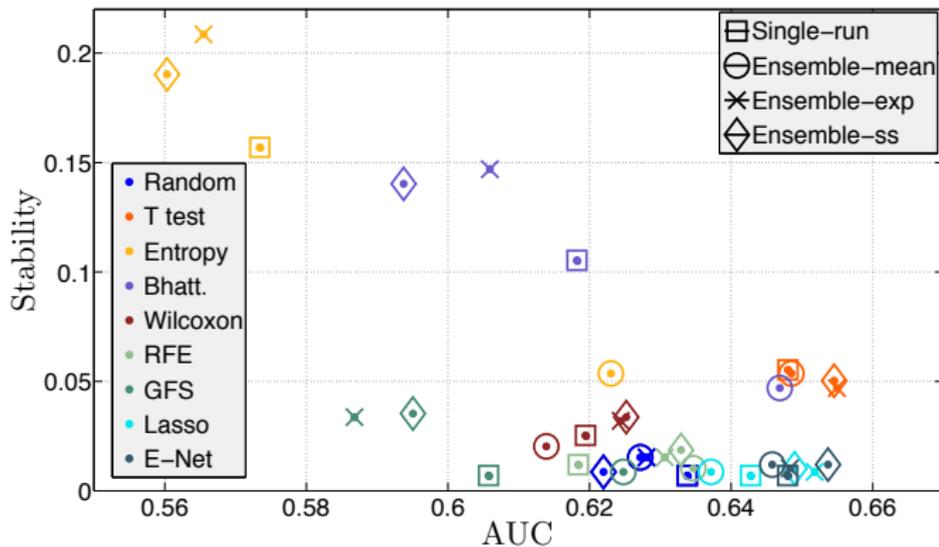
OPEN ACCESS Freely available online

PLoS one

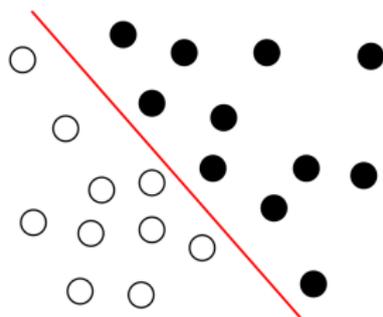
## The Influence of Feature Selection Methods on Accuracy, Stability and Interpretability of Molecular Signatures

Anne-Claire Haury<sup>1,2,3\*</sup>, Pierre Gestraud<sup>1,2,3</sup>, Jean-Philippe Vert<sup>1,2,3</sup>

**1** Mines ParisTech, Centre for Computational Biology, Fontainebleau, France, **2** Institut Curie, Paris, France, **3** Institut National de la Santé et de la Recherche Médicale, Paris, France



# Learning with regularization



For a sample  $x \in \mathbb{R}^p$ , learn a linear decision function:

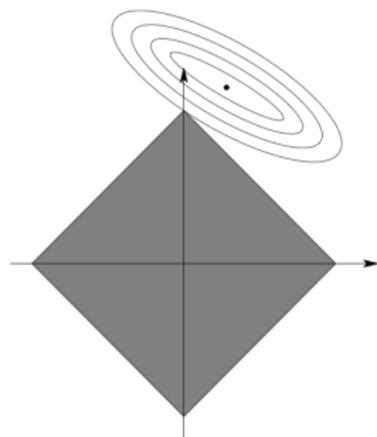
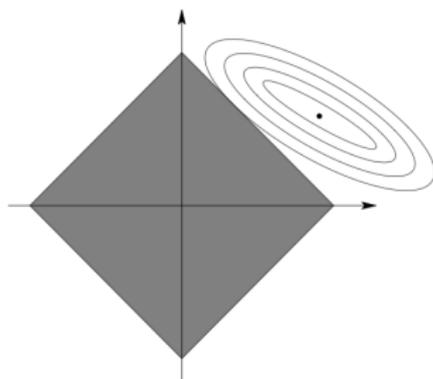
$$f_{\beta}(x) = \beta^{\top} x \quad \min_{\beta \in \mathbb{R}^p} R(f_{\beta}) + \lambda \Omega(\beta)$$

- $R(f_{\beta})$  empirical risk, e.g.,  $R(f_{\beta}) = \frac{1}{n} \sum_{i=1}^n (f_{\beta}(x_i) - y_i)^2$
- $\Omega(\beta)$  **penalty**, to control overfitting in high dimension, e.g.:
  - $\Omega(\beta) = \sum_{i=1}^p \beta_i^2$  (ridge regression, SVM,...)
  - $\Omega(\beta) = \sum_{i=1}^p |\beta_i|$  (lasso, boosting,...)

# Sparsity with $\ell_1$ regularization

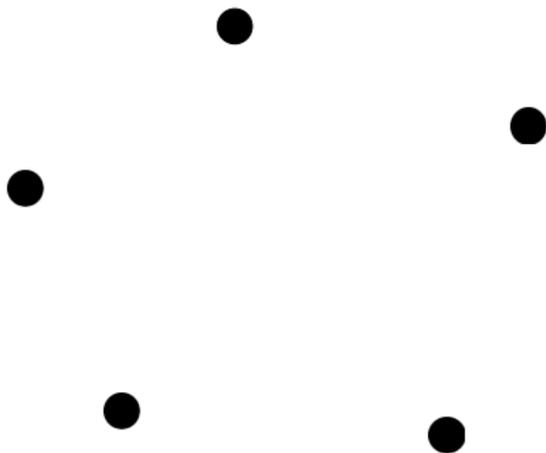
$$\min_{\beta} R(f_{\beta}) + \lambda \sum_{i=1}^p |\beta_i| \Leftrightarrow \min_{\beta} R(f_{\beta}) \text{ such that } \sum_{i=1}^p |\beta_i| \leq C$$

Geometric interpretation with  $p = 2$



Leads to **sparse** models (feature selection)

# Atomic Norm (Chandrasekaran et al., 2012)



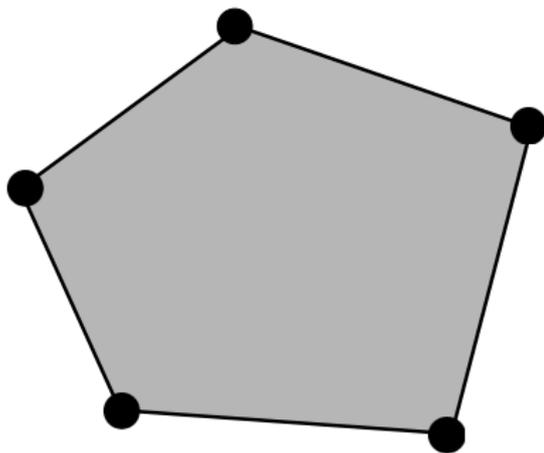
## Definition

Given a set of atoms  $\mathcal{A}$ , the associated atomic norm is

$$\|x\|_{\mathcal{A}} = \inf\{t > 0 \mid x \in t \operatorname{conv}(\mathcal{A})\}.$$

$\mathcal{A}$  should be centrally symmetric and span  $\mathbb{R}^p$

# Atomic Norm (Chandrasekaran et al., 2012)



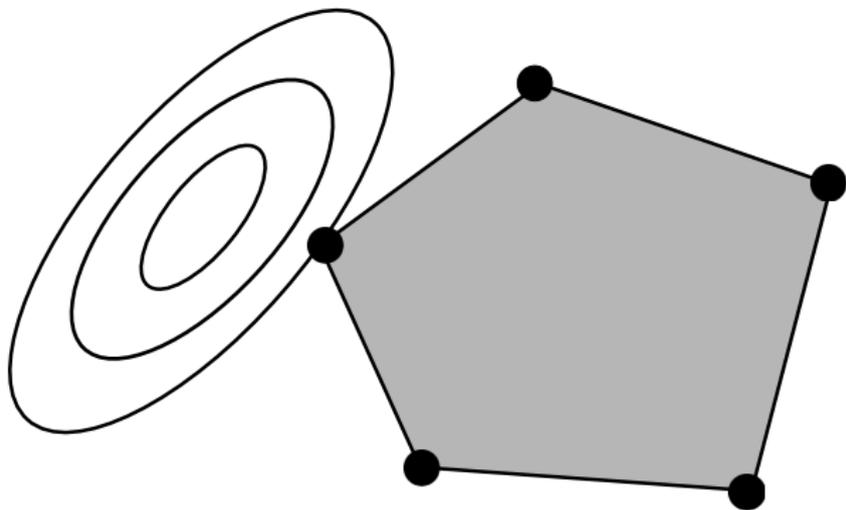
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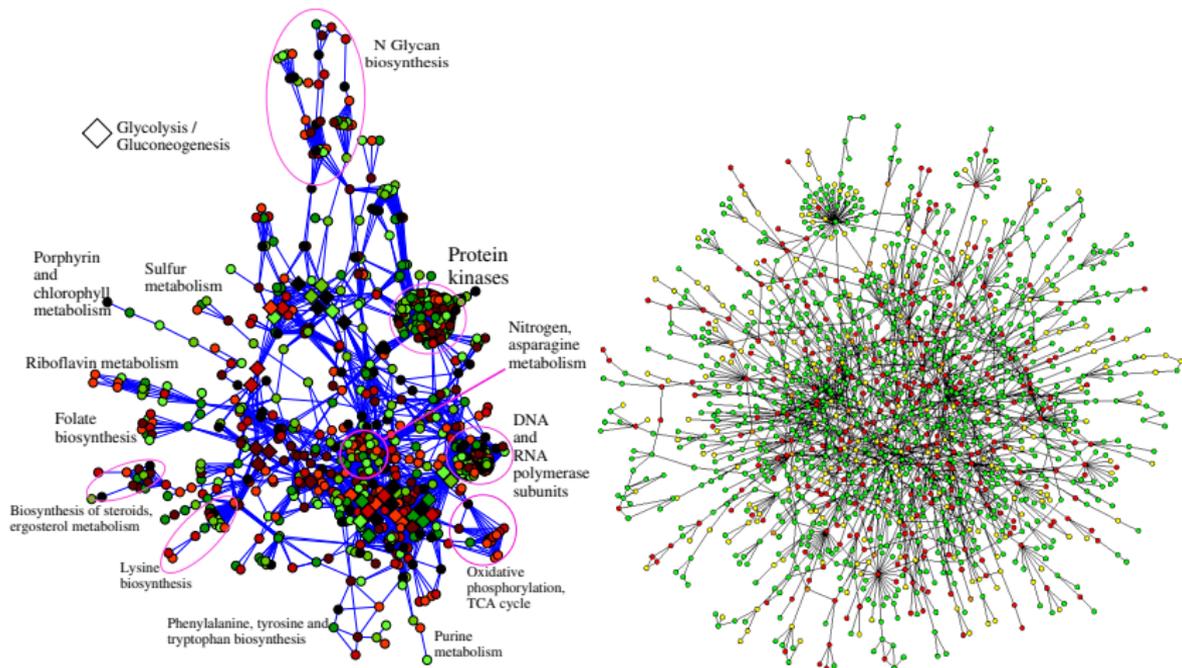
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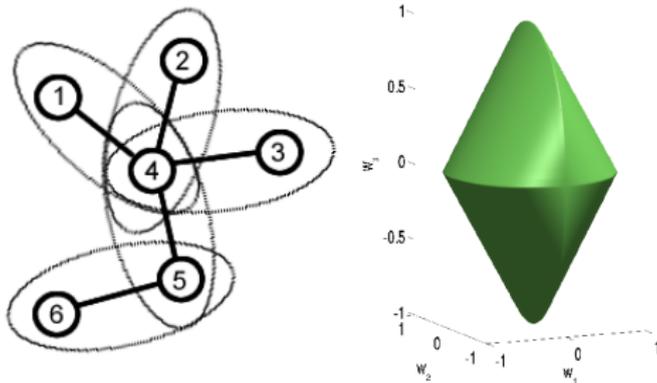
$\mathcal{A}$  should be centrally symmetric and span  $\mathbb{R}^p$

# Gene networks as prior knowledge



Let's force the signatures to be "coherent" with a known gene network?

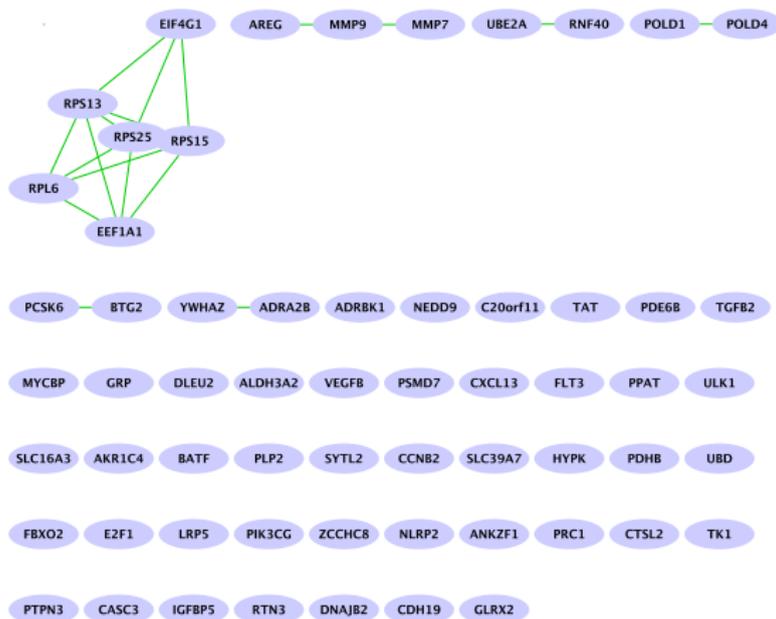
# Graph lasso (Jacob et al., 2009)



$$\Omega(\beta) = \sup_{\alpha \in \mathbb{R}^p: \forall i \sim j, \|\alpha_i^2 + \alpha_j^2\| \leq 1} \alpha^\top \beta$$

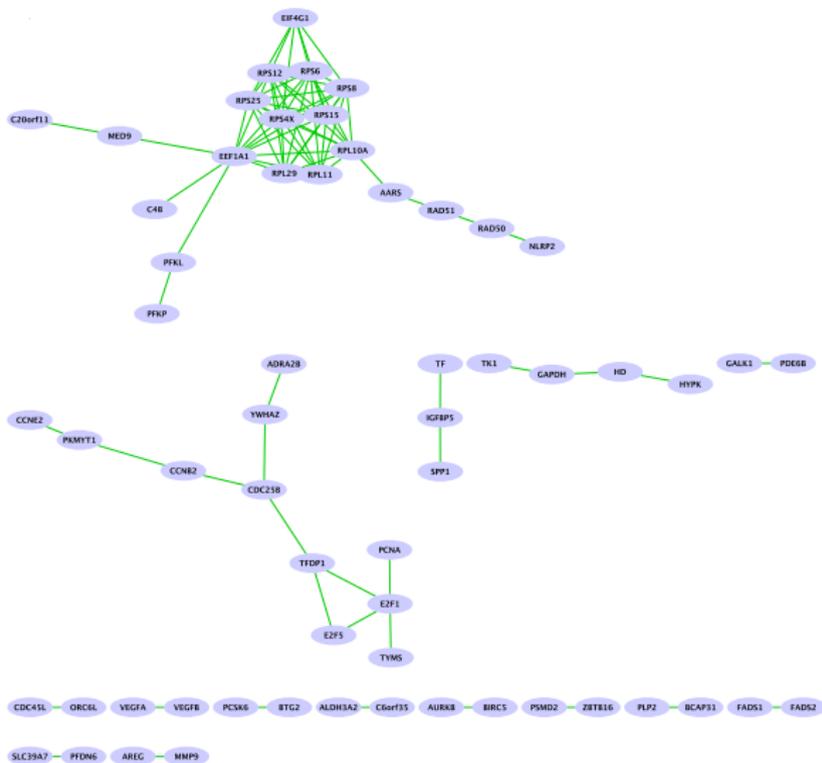


# Lasso signature (accuracy 0.61)



*Breast cancer prognosis, Jacob et al. (2009)*

# Graph Lasso signature (accuracy 0.64)

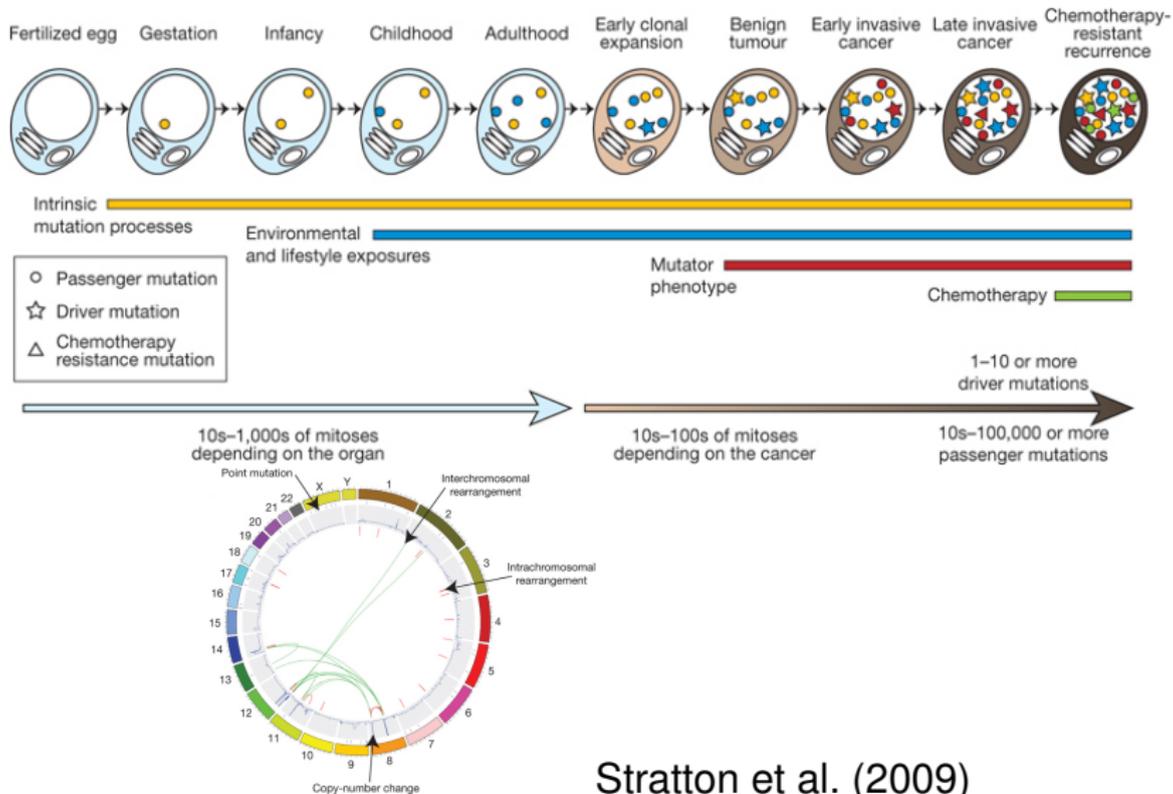


*Breast cancer prognosis, Jacob et al. (2009)*

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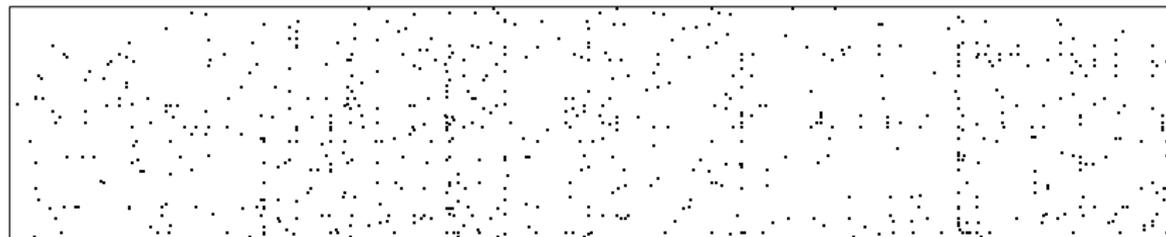
# Somatic mutations in cancer



Stratton et al. (2009)

# Large-scale efforts to collect somatic mutations

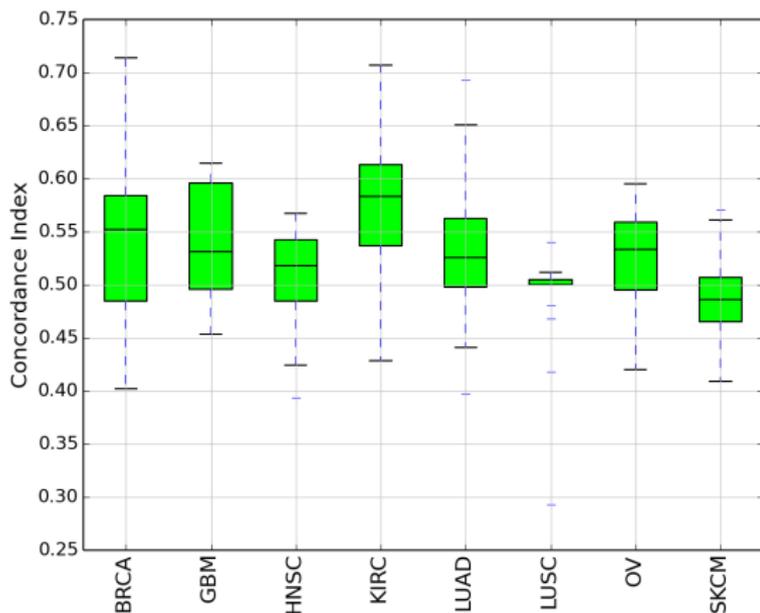
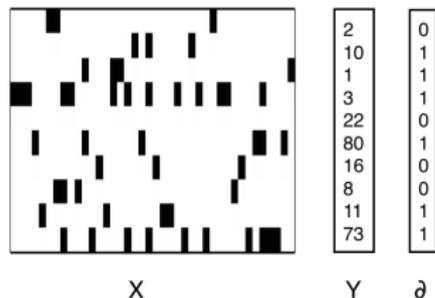
- 3,378 samples with survival information from 8 cancer types
- downloaded from the TCGA / cBioPortal portals.



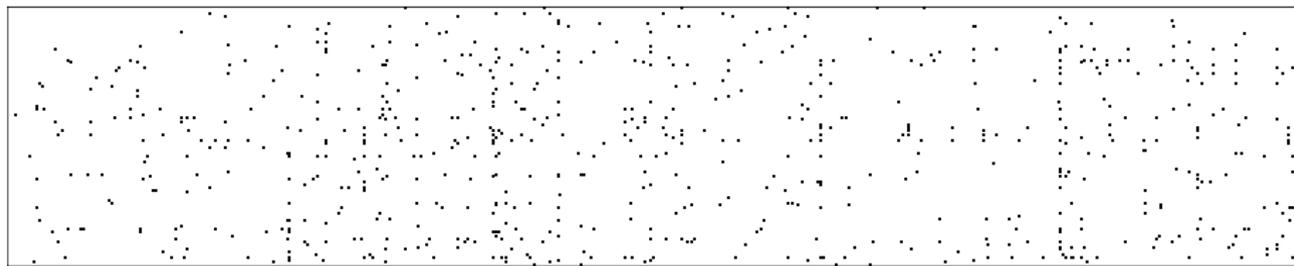
Cancer type	Patients	Genes
LUAD (Lung adenocarcinoma)	430	20 596
SKCM (Skin cutaneous melanoma)	307	17 463
GBM (Glioblastoma multiforme)	265	14 750
BRCA (Breast invasive carcinoma)	945	16 806
KIRC (Kidney renal clear cell carcinoma)	411	10 609
HNSC (Head and Neck squamous cell carcinoma)	388	17 022
LUSC (Lung squamous cell carcinoma)	169	13 590
OV (Ovarian serous cystadenocarcinoma)	363	10 195

# Survival prediction from raw mutation profiles

- Each patient is a **binary vector**: each gene is mutated (1) or not (2)
- Silent mutations are removed
- Survival model estimated with sparse survival SVM
- Results on 5-fold cross-validation repeated 4 times



# Changing the representation?



Can we replace

$x \in \{0, 1\}^p$  with  $p$  very large, very sparse

by a representation with more information shared between samples

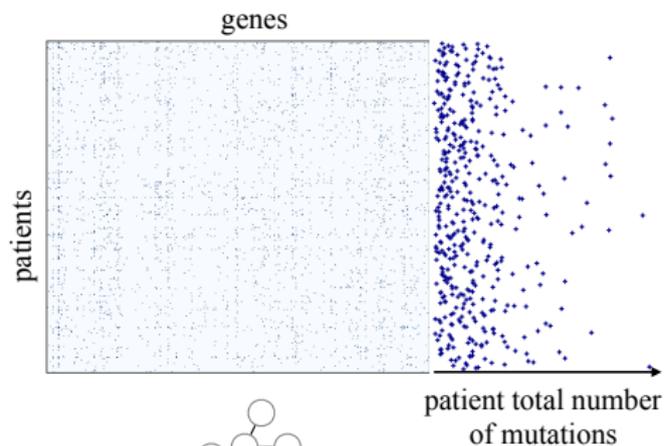
$\Phi(x) \in \mathcal{H}$  ?



# NetNorm Overview (Le Morvan et al., 2016)

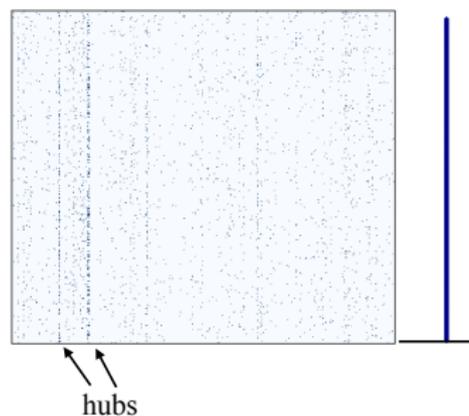
- **Modify** the binary vector  $x \in \{0, 1\}^p$  of each patient by **adding or removing mutations**, using a **gene network** as prior knowledge
- After Netnorm, all patients  $\Phi(x) \in \{0, 1\}^p$  have the **same number of (pseudo-)mutations**

Raw binary mutation matrix



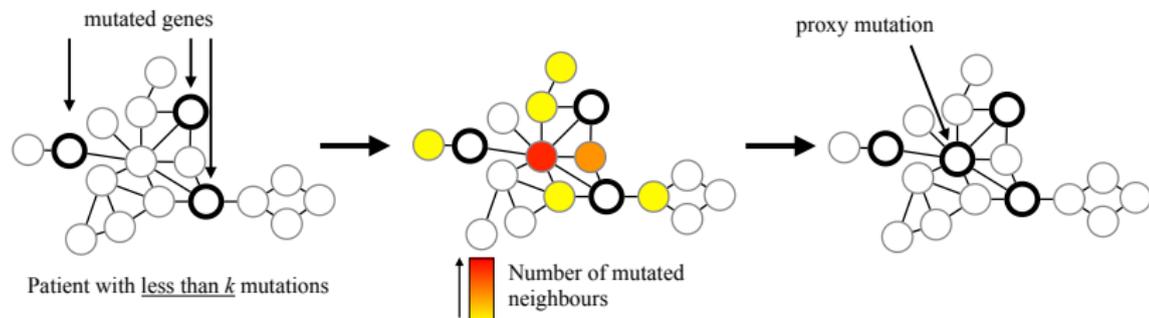
Gene-gene interaction network

NetNorM binary mutation matrix

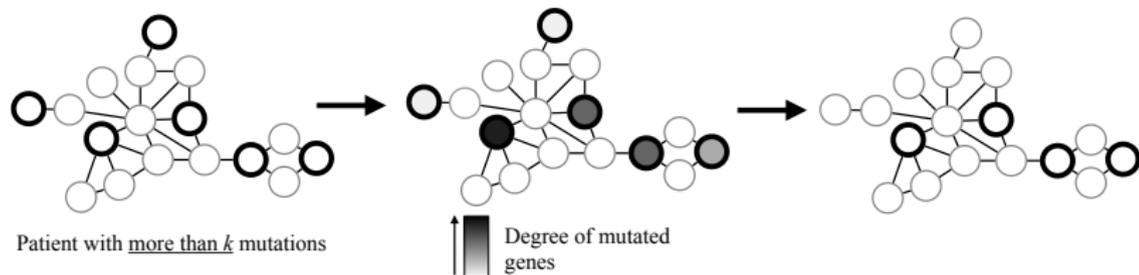


# NetNorm detail ( $k=4$ )

- 1 **Add** mutations for patients with **few** (less than  $k$ ) mutations



- 2 **Remove** mutations for patients for **many** (more than  $k$ ) mutations



## Network-based stratification of tumor mutations

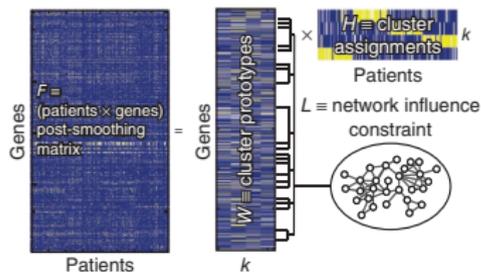
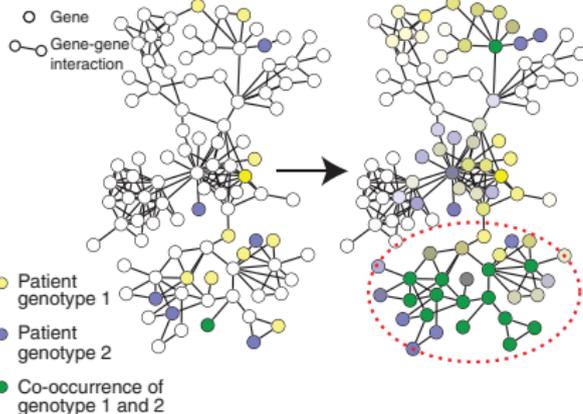
Matan Hofree<sup>1</sup>, John P Shen<sup>2</sup>, Hannah Carter<sup>2</sup>, Andrew Gross<sup>3</sup> & Trey Ideker<sup>1-3</sup>

<sup>1</sup>Department of Computer Science and Engineering, University of California, San Diego, La Jolla, California, USA. <sup>2</sup>Department of Medicine, University of California, San Diego, La Jolla, California, USA. <sup>3</sup>Department of Bioengineering, University of California, San Diego, La Jolla, California, USA. Correspondence should be addressed to T.I. ([tideker@ucsd.edu](mailto:tideker@ucsd.edu)).

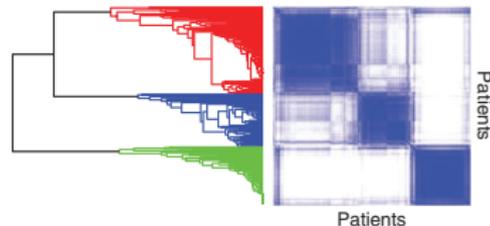
RECEIVED 14 FEBRUARY; ACCEPTED 12 AUGUST; PUBLISHED ONLINE 15 SEPTEMBER 2013; DOI:10.1038/NMETH.2651

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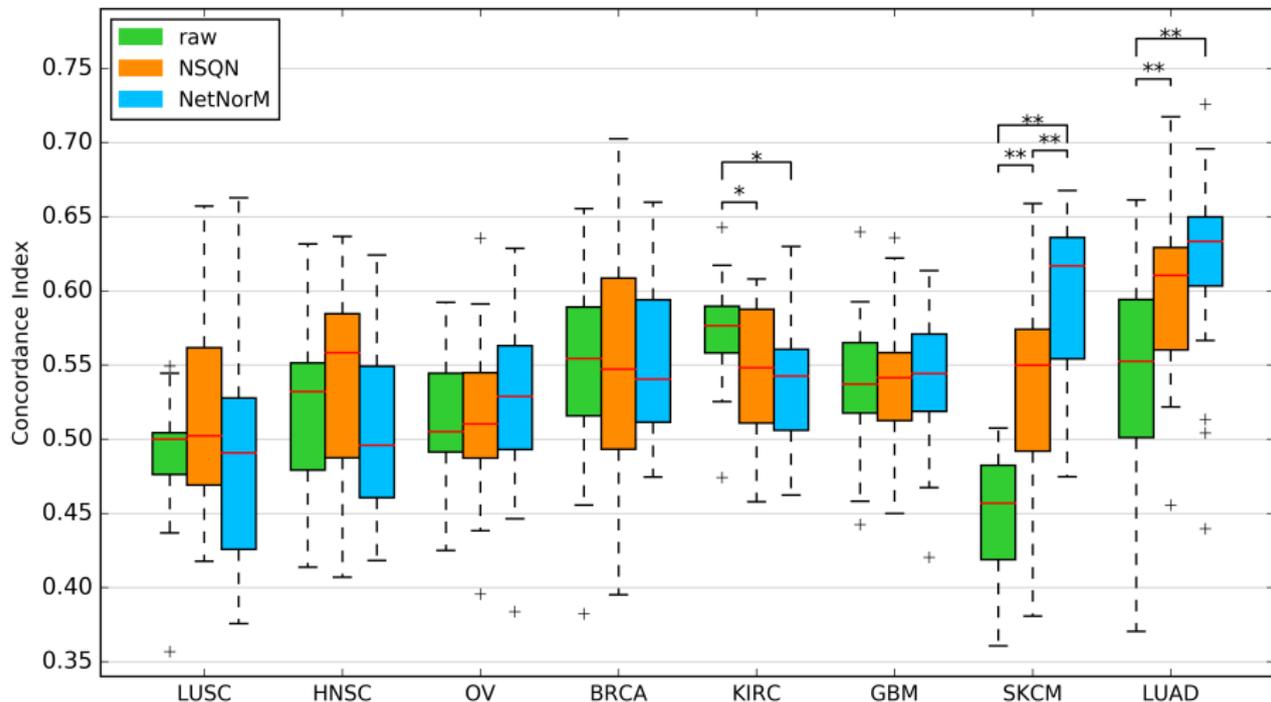
Network smoothing:



d Network-based stratification



# Performance on survival prediction



*Use Pathway Commons as gene network.*

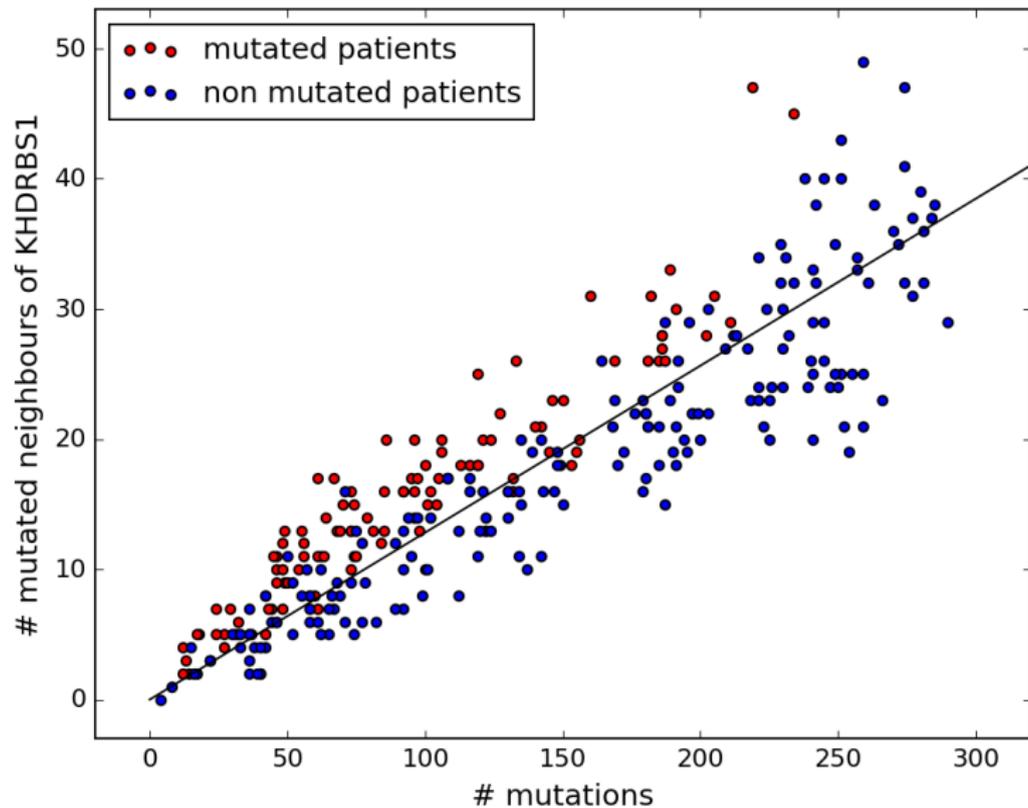
*NSQN = Network Smoothing / Quantile Normalization (Hofree et al., 2013)*

# Selected genes represent "true" or "proxy" mutations

	freq	coef	$m_{all}$		$m_{<k_{med}}$		$m_{\geq k_{med}}$		Log-rank test (p-value)		Welsh t-test (p-value)	
			raw	NetNorM	raw	NetNorM	raw	NetNorM	raw	NetNorM	raw	NetNorM
TP53	19	-0.16	238	274	123	159	115	115	$7.6 \times 10^{-2}$	$9.4 \times 10^{-2}$	$5.2 \times 10^{-22}$	$1.2 \times 10^{-13}$
CRB1	18	-0.4	44	38	22	22	22	16	$1.6 \times 10^{-4}$	$1.4 \times 10^{-6}$	$9.9 \times 10^{-4}$	$6.9 \times 10^{-2}$
NOTCH4	17	-0.23	42	26	14	14	28	12	$9.3 \times 10^{-1}$	$3.3 \times 10^{-2}$	$1.9 \times 10^{-6}$	$2.6 \times 10^{-1}$
ANK2	17	0.1	90	90	33	33	57	57	$1.2 \times 10^{-2}$	$1.2 \times 10^{-2}$	$6.3 \times 10^{-10}$	$6.3 \times 10^{-10}$
RPS9	16	0.38	0	106	0	106	0	0	-	$1.8 \times 10^{-1}$	-	$4.2 \times 10^{-47}$
LAMA2	15	0.16	52	38	14	15	38	23	$1.5 \times 10^{-2}$	$2.3 \times 10^{-2}$	$6.3 \times 10^{-9}$	$2.6 \times 10^{-3}$
RYR2	14	0.07	165	161	70	70	95	91	$1.4 \times 10^{-2}$	$2.1 \times 10^{-2}$	$6.7 \times 10^{-19}$	$1 \times 10^{-15}$
IGF2BP2	14	-0.15	6	67	2	63	4	4	$1.4 \times 10^{-5}$	$3.6 \times 10^{-3}$	$1 \times 10^{-1}$	$6.8 \times 10^{-7}$
SMARCA5	14	-0.09	5	137	1	133	4	4	$2.1 \times 10^{-1}$	$5.3 \times 10^{-3}$	$1.3 \times 10^{-1}$	$1 \times 10^{-27}$
KHDRBS1	13	0.11	7	117	2	112	5	5	$7.1 \times 10^{-1}$	$9.7 \times 10^{-1}$	$6.5 \times 10^{-2}$	$1.3 \times 10^{-18}$
YWHAZ	13	-0.18	2	241	0	239	2	2	$2.5 \times 10^{-31}$	$6.1 \times 10^{-4}$	$4.7 \times 10^{-1}$	$4.4 \times 10^{-37}$
HRNR	13	-0.12	62	64	20	22	42	42	$1.1 \times 10^{-1}$	$1.1 \times 10^{-1}$	$6 \times 10^{-10}$	$2.9 \times 10^{-9}$
CSNK2A2	11	0.06	2	129	1	128	1	1	$9 \times 10^{-1}$	$8.8 \times 10^{-1}$	$5.9 \times 10^{-1}$	$4.2 \times 10^{-27}$
MED12L	11	0.04	27	27	8	8	19	19	$5.5 \times 10^{-2}$	$5.5 \times 10^{-2}$	$1.7 \times 10^{-4}$	$1.7 \times 10^{-4}$

- 14 genes are selected at least 50% of the time
- 6/14 are "proxy" genes (in blue)
  - big hubs in the network
  - get mutated by NetNorm in patients with few mutations  $\implies$  they encode the mutation rate
- 8/14 are "normal" prognostic genes

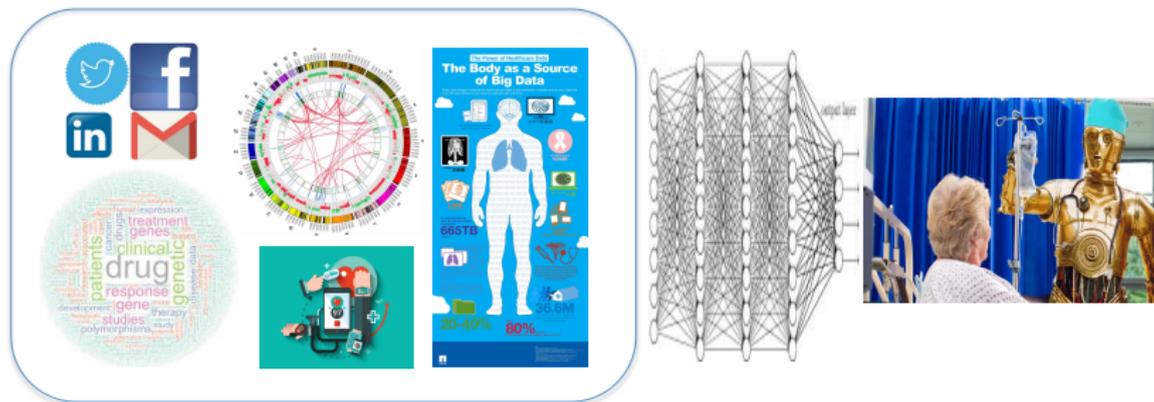
# Proxy mutations encode local mutational burden



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# Conclusion



- Many **new exciting problems** and **lots of data** in computational genomics and precision medicine
- $n \ll p$  problem requires dedicated methods
  - new **representations**  $x \rightarrow \Phi(x)$
  - new **learning techniques** (structured sparsity, regularization, ...)

# Thanks



# References

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