

Machine learning from precision medicine

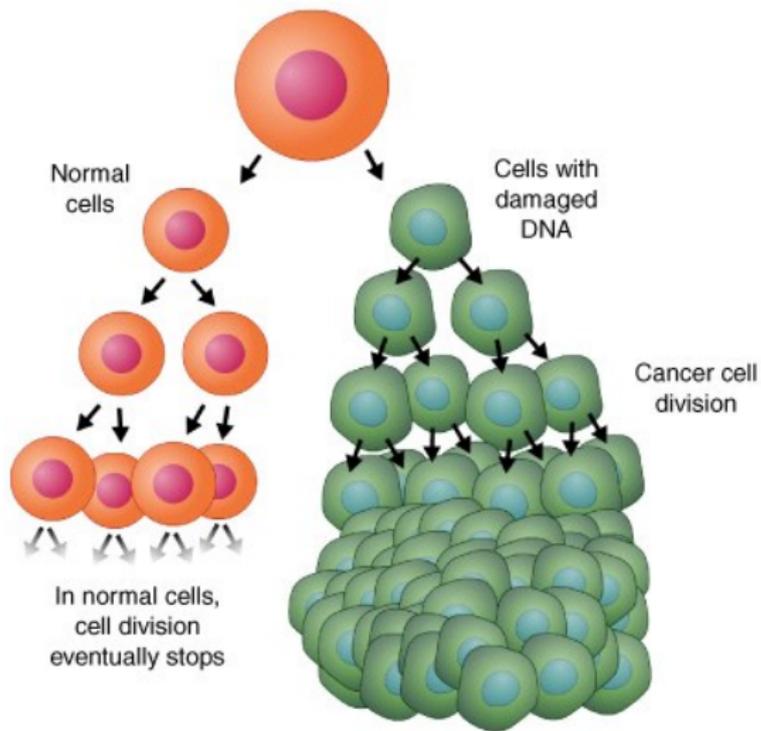
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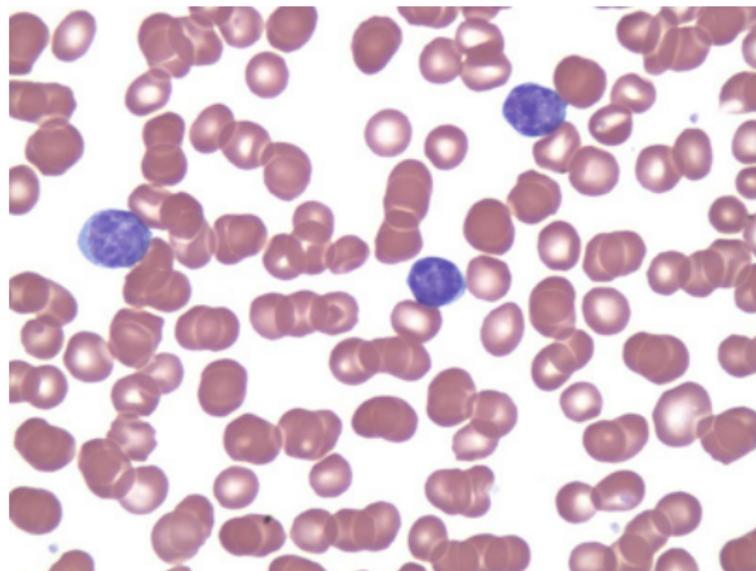


Krupp Symposium "From Machine Learning to Personalize
Medicine", Munich, October 21, 2016

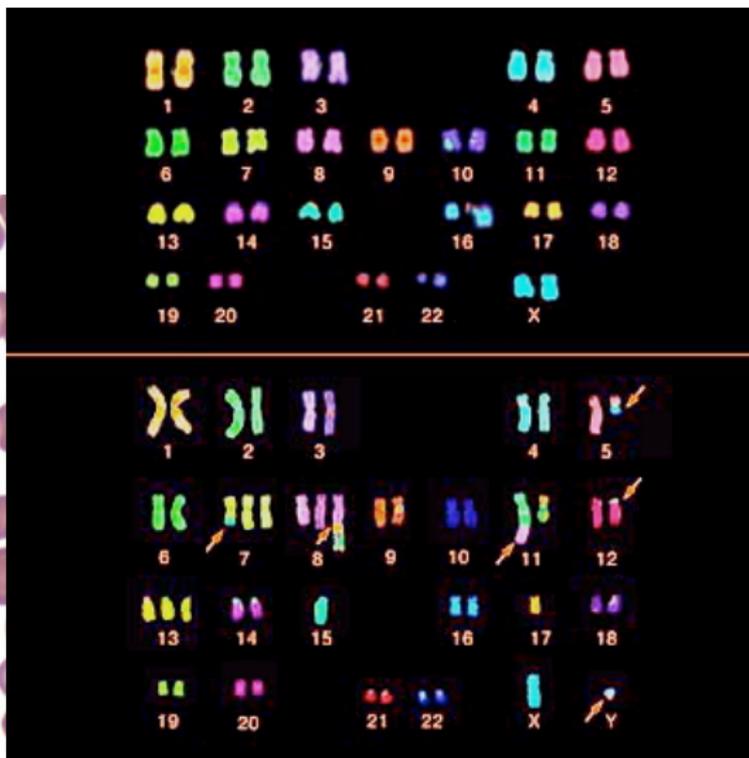
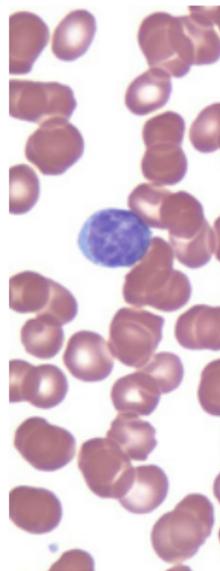
Cancer



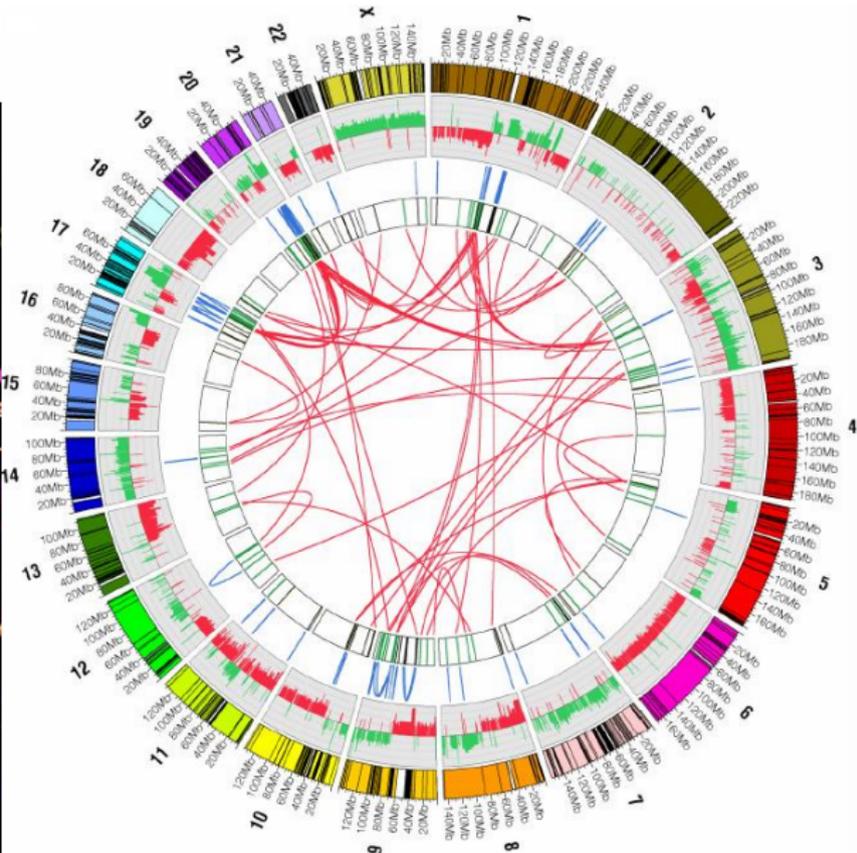
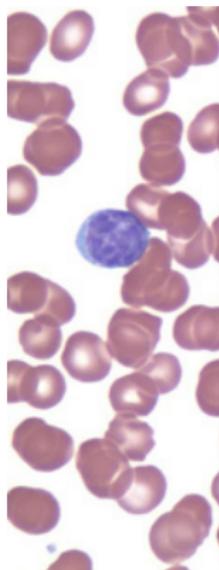
A cancer cell (1900)



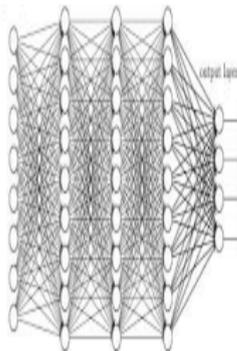
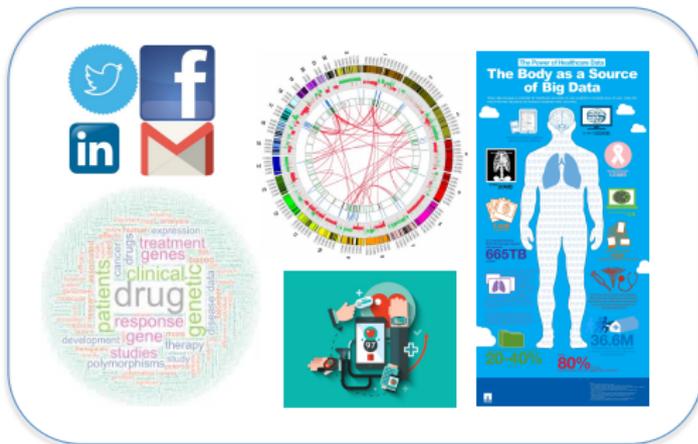
A cancer cell (1960)



A cancer cell (2010)



Opportunities



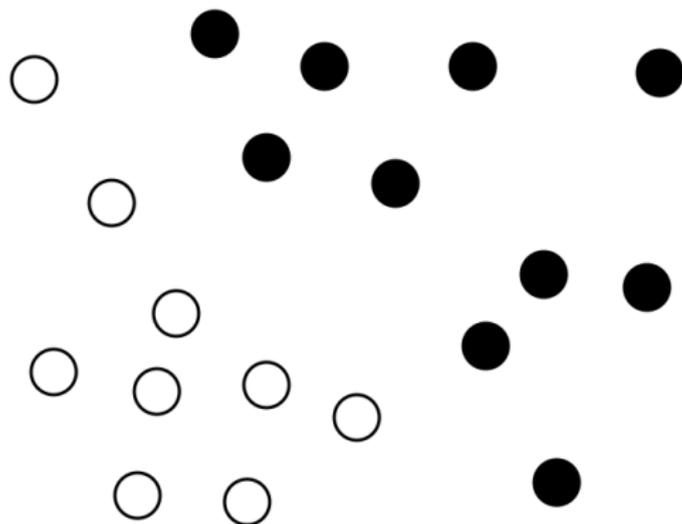
- What is your risk of developing a cancer? (*prevention*)
- Once detected, what precisely is your cancer? (*diagnosis*)
- After treatment, are you cured? (*prognosis*)
- What is the best way to treat your cancer? (*precision medicine*)

Example: precision medicine



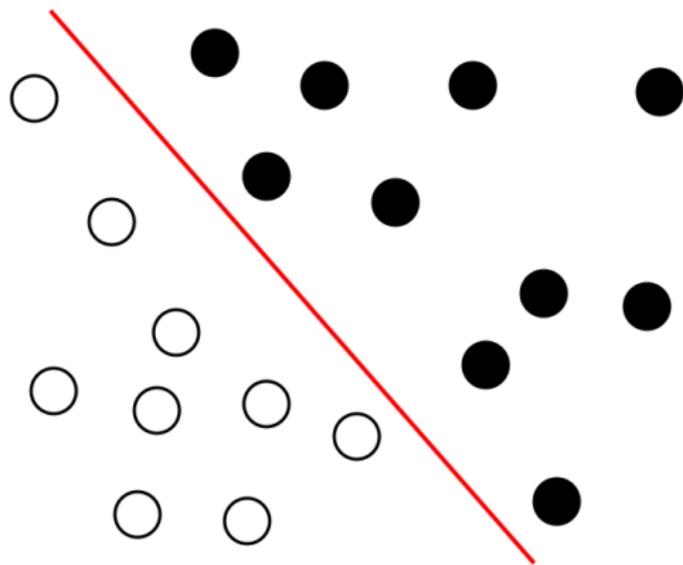
Learning from data (EASY case)

- Good vs Bad responders
- $n(= 19)$ patients \gg $p(= 2)$ genes



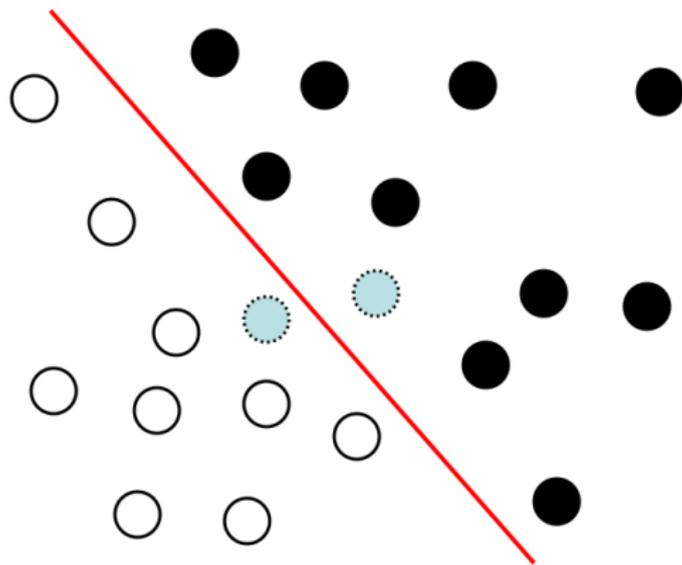
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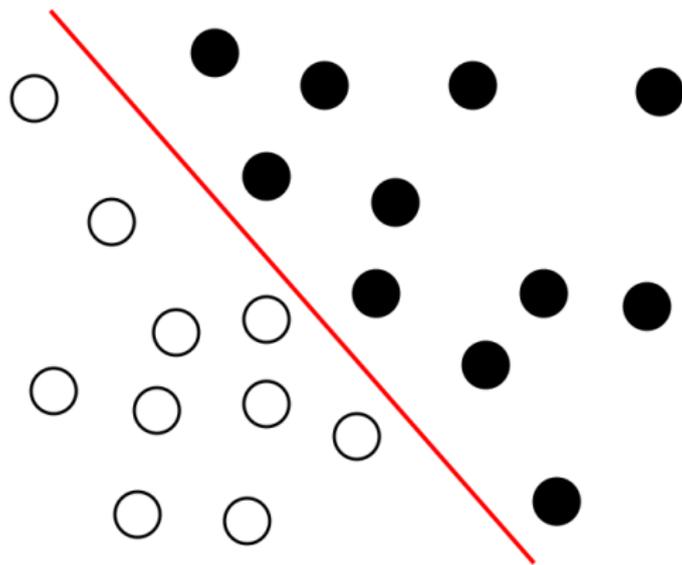
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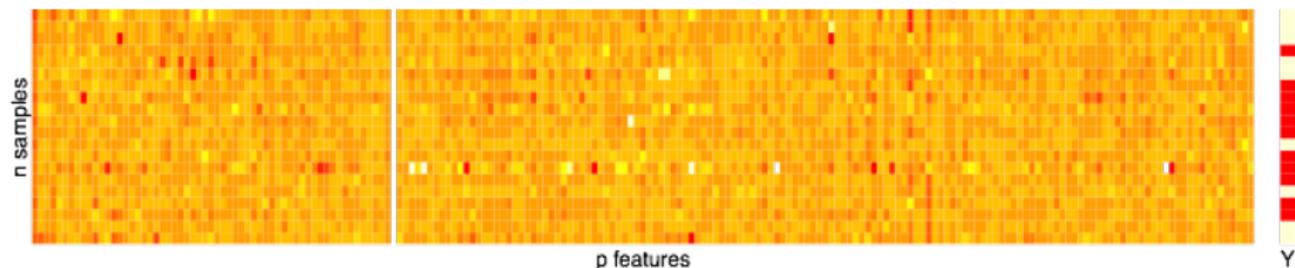


Learning from data (EASY case)

- Good vs Bad responders
- $n(= 19)$ patients \gg $p(= 2)$ genes



*-omics challenge: $n \ll p$



- $n = 10^2 \sim 10^4$ (patients)
- $p = 10^4 \sim 10^7$ (genes, mutations, copy number, ...)
- Data of **various nature** (continuous, discrete, structured, ...)
- Data of **variable quality** (technical/batch variations, noise, ...)

Consequences:

- Accuracy drops
- Biomarker selection unstable
- Speed and scalability can become an issue

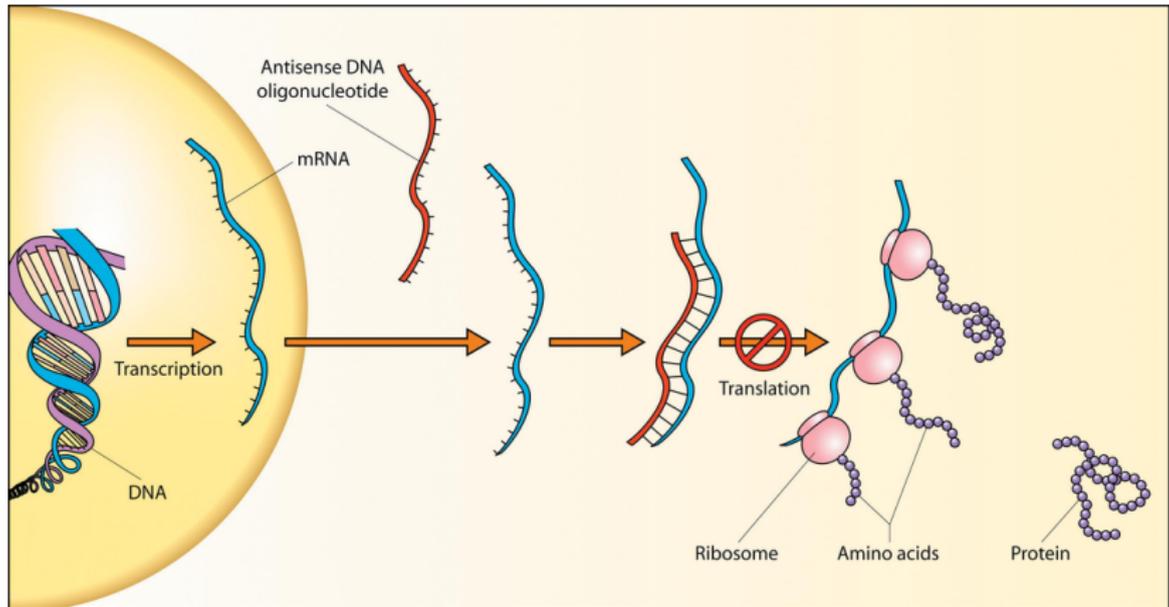
Outline

- 1 Learning from gene expression data
- 2 Learning from mutation data
- 3 Conclusion

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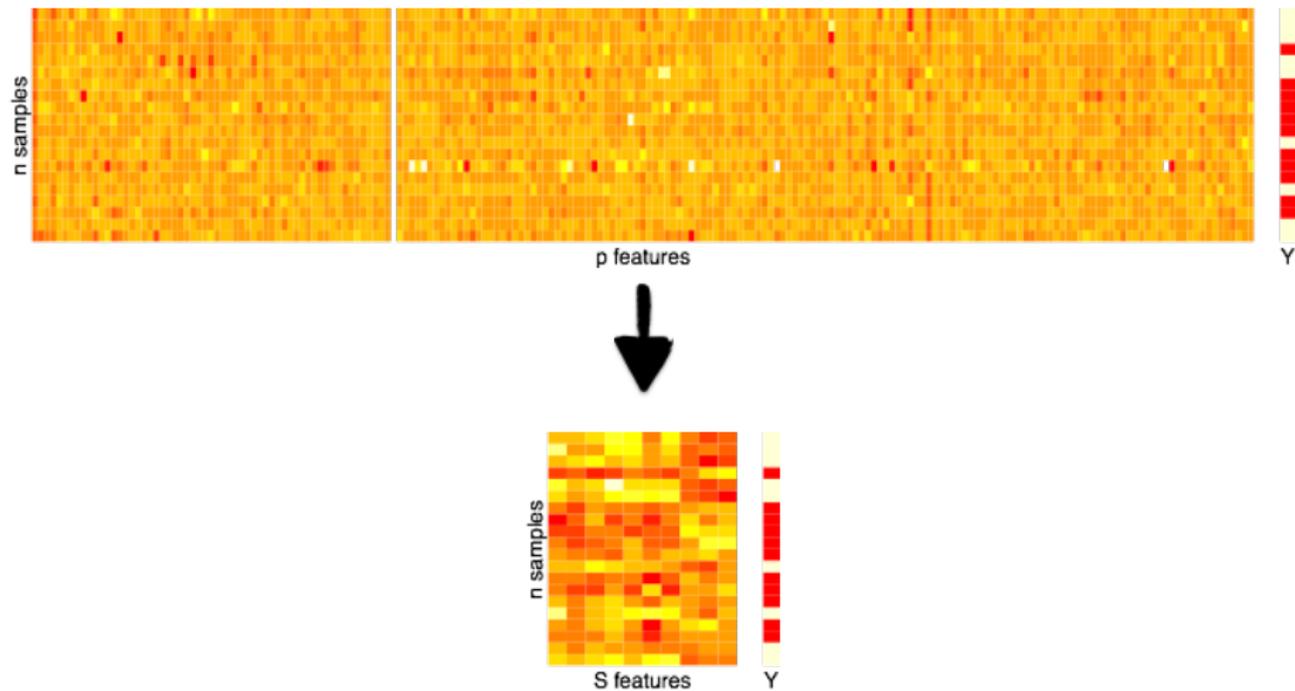
Gene expression



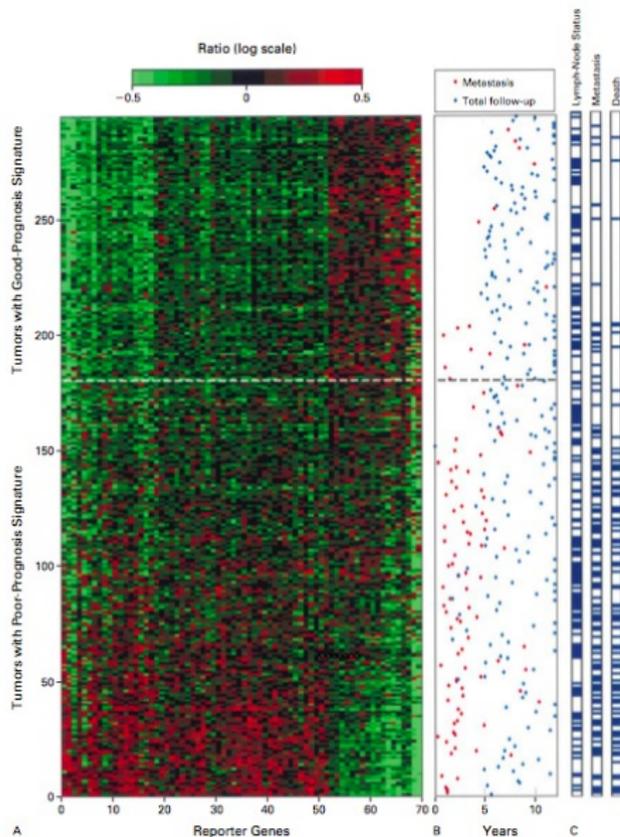
<http://mrsbabbkv.weebly.com/rna--protein.html>

- About 22,000 genes encoded in DNA (same for all cells)
- Expression of each gene (= RNA synthesis) varies between cells
- Can be measured for all genes simultaneously with sequencing

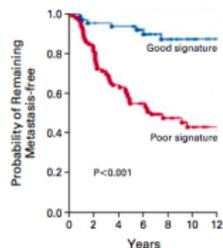
Feature selection (a.k.a. *molecular signature*)



Example: 70-gene breast cancer prognostic signature



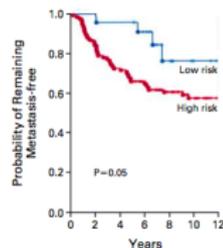
A Gene-Expression Profiling



No. At Risk

Good signature	60	57	54	45	31	22	12
Poor signature	91	72	55	41	26	17	9

B St. Gallen Criteria



No. At Risk

Low risk	22	22	21	17	9	5	2
High risk	129	107	88	69	48	34	19



van 't Veer et al. (2002);
van de Vijver et al. (2002)

But...

Gene expression profiling predicts clinical outcome of breast cancer

Laura J. van 't Veer*†, Hongyue Dai†‡, Marc J. van de Vijver*†, Yudong D. He‡, Augustinus A. M. Hart*, Mao Mao‡, Hans L. Peterse*, Karin van der Kooy*, Matthew J. Marton‡, Anke T. Witteveen*, George J. Schreiber‡, Ron M. Kerkhoven*, Chris Roberts‡, Peter S. Linsley‡, René Bernards* & Stephen H. Friend‡

* Divisions of Diagnostic Oncology, Radiotherapy and Molecular Carcinogenesis and Center for Biomedical Genetics, The Netherlands Cancer Institute, 121 Plesmanlaan, 1066 CX Amsterdam, The Netherlands
‡ Rosetta Inpharmatics, 12040 115th Avenue NE, Kirkland, Washington 98034.

70 genes (Nature, 2002)

Gene-expression profiles to predict distant metastasis of lymph-node-negative primary breast cancer

Yixin Wang, Jan G M Kljijn, Yi Zhang, Anieta M Sieuwerts, Maxime P Look, Fei Yang, Dmitri Talantov, Mieke Timmermans, Marion E Meijer-van Gelder, Jack Yu, Tim Jatko, Els M J J Berns, David Atkins, John A Foekens

76 genes (Lancet, 2005)

3 genes in common

van 't Veer et al. (2002); Wang et al. (2005)

3 genes is the best you can expect given n and p

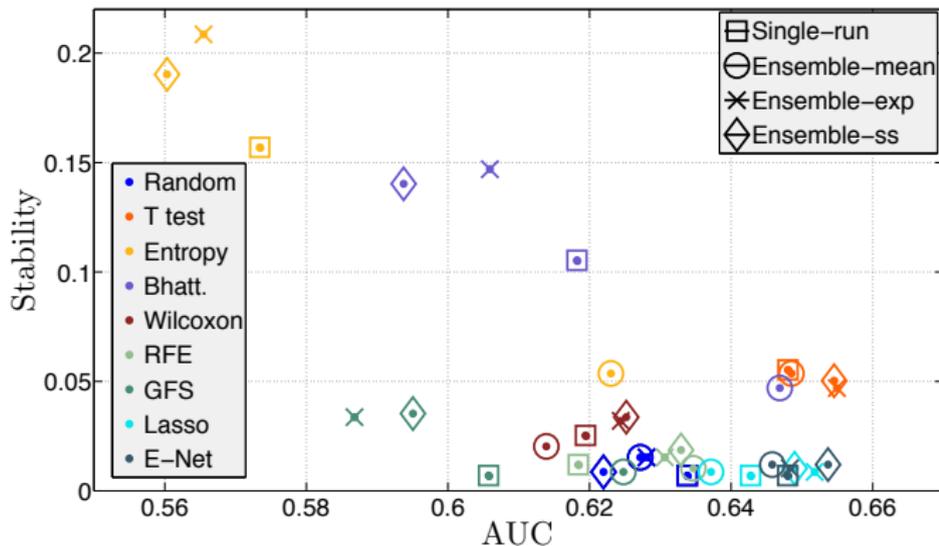
OPEN ACCESS Freely available online

PLoS one

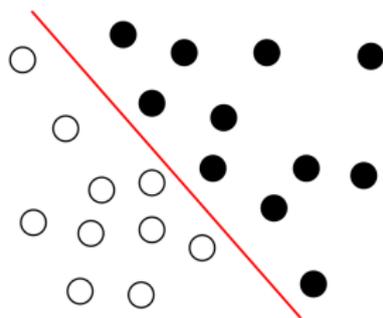
The Influence of Feature Selection Methods on Accuracy, Stability and Interpretability of Molecular Signatures

Anne-Claire Haury^{1,2,3*}, Pierre Gestraud^{1,2,3}, Jean-Philippe Vert^{1,2,3}

1 Mines ParisTech, Centre for Computational Biology, Fontainebleau, France, **2** Institut Curie, Paris, France, **3** Institut National de la Santé et de la Recherche Médicale, Paris, France



Learning with regularization



For a sample $x \in \mathbb{R}^p$, learn a linear decision function:

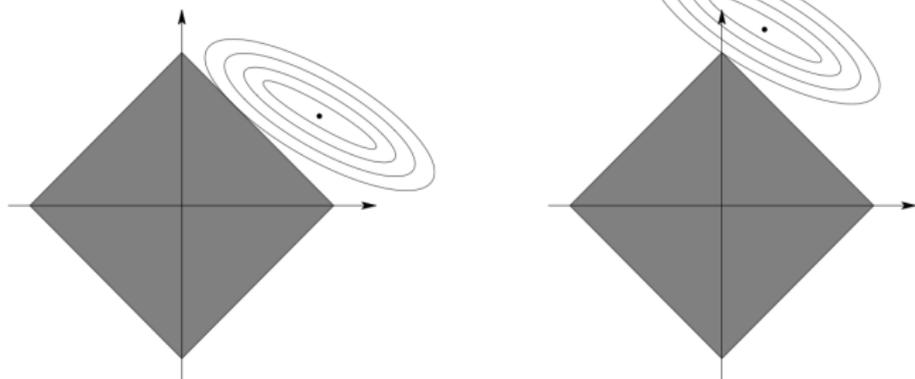
$$f_{\beta}(x) = \beta^{\top} x \quad \min_{\beta \in \mathbb{R}^p} R(f_{\beta}) + \lambda \Omega(\beta)$$

- $R(f_{\beta})$ empirical risk, e.g., $R(f_{\beta}) = \frac{1}{n} \sum_{i=1}^n (f_{\beta}(x_i) - y_i)^2$
- $\Omega(\beta)$ **penalty**, to control overfitting in high dimension, e.g.:
 - $\Omega(\beta) = \sum_{i=1}^p \beta_i^2$ (ridge regression, SVM,...)
 - $\Omega(\beta) = \sum_{i=1}^p |\beta_i|$ (lasso, boosting,...)

Sparsity with ℓ_1 regularization

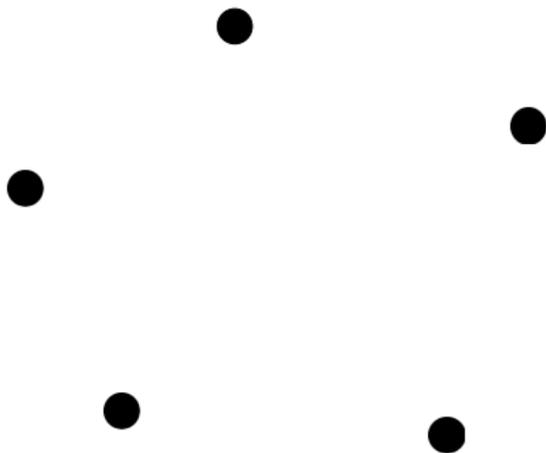
$$\min_{\beta} R(f_{\beta}) + \lambda \sum_{i=1}^p |\beta_i| \Leftrightarrow \min_{\beta} R(f_{\beta}) \text{ such that } \sum_{i=1}^p |\beta_i| \leq C$$

Geometric interpretation with $p = 2$



Leads to **sparse** models (feature selection)

Atomic Norm (Chandrasekaran et al., 2012)



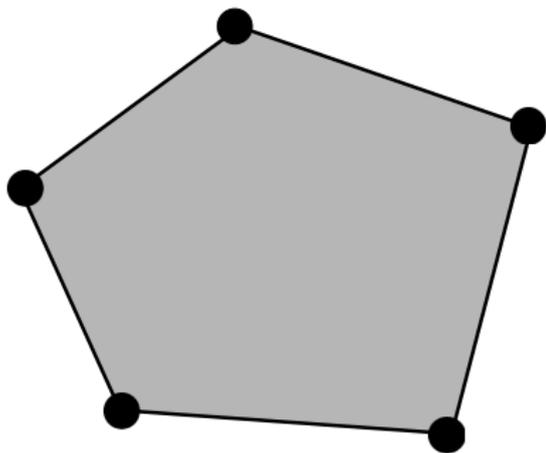
Definition

Given a set of atoms \mathcal{A} , the associated atomic norm is

$$\|x\|_{\mathcal{A}} = \inf\{t > 0 \mid x \in t \operatorname{conv}(\mathcal{A})\}.$$

\mathcal{A} should be centrally symmetric and span \mathbb{R}^p

Atomic Norm (Chandrasekaran et al., 2012)



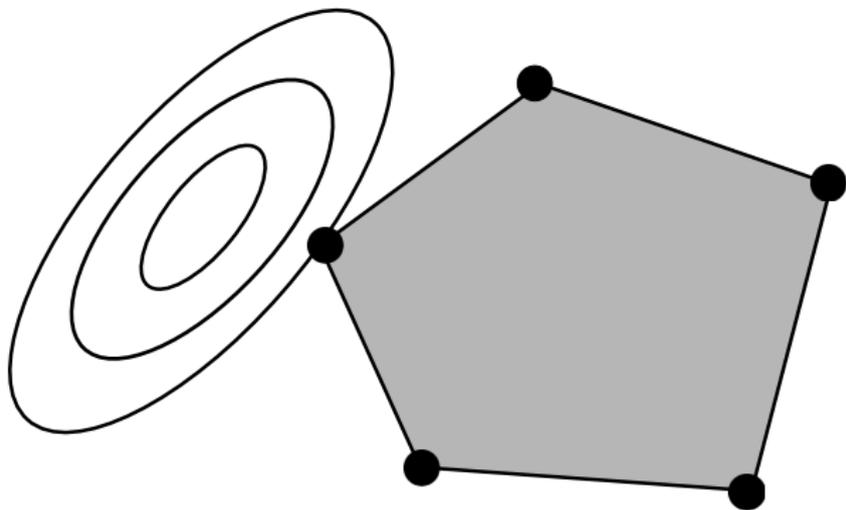
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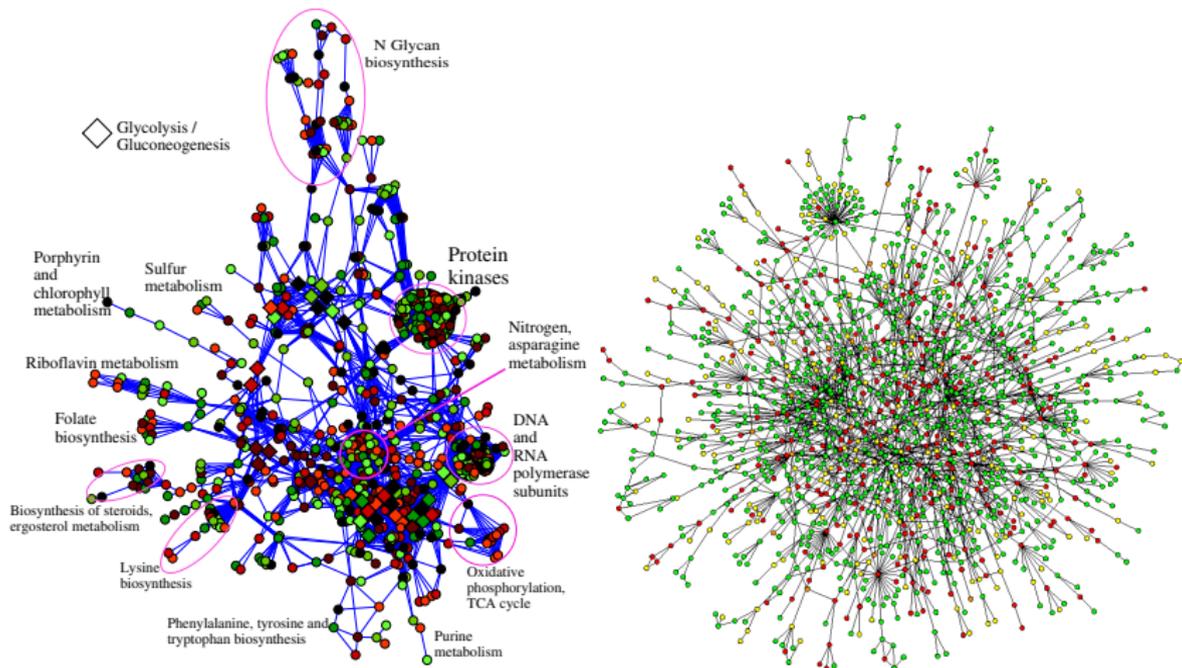
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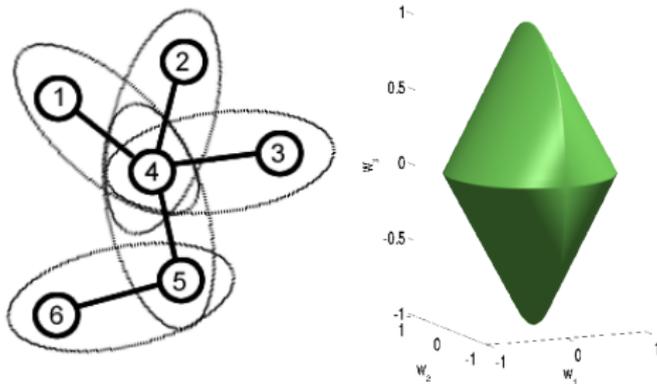
\mathcal{A} should be centrally symmetric and span \mathbb{R}^p

Gene networks as prior knowledge



Let's force the signatures to be "coherent" with a known gene network?

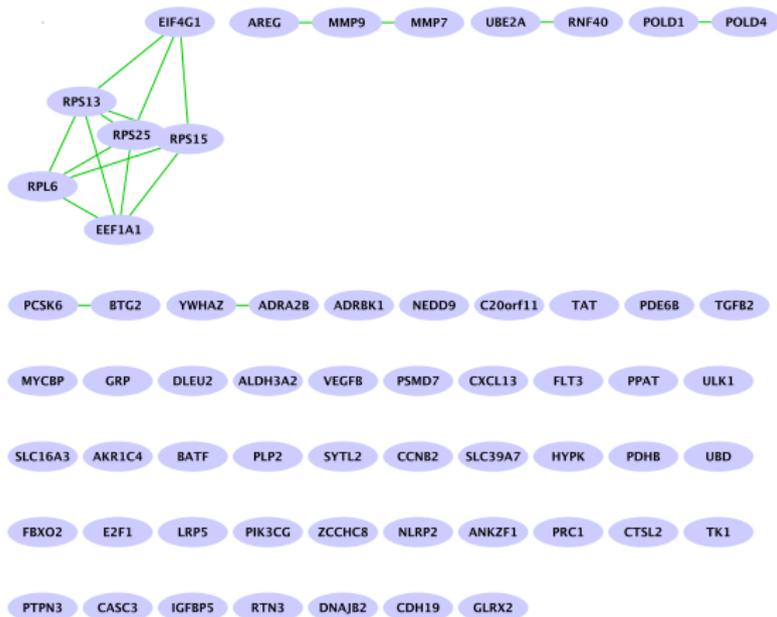
Graph lasso (Jacob et al., 2009)



$$\Omega(\beta) = \sup_{\alpha \in \mathbb{R}^p: \forall i \sim j, \|\alpha_i^2 + \alpha_j^2\| \leq 1} \alpha^\top \beta$$

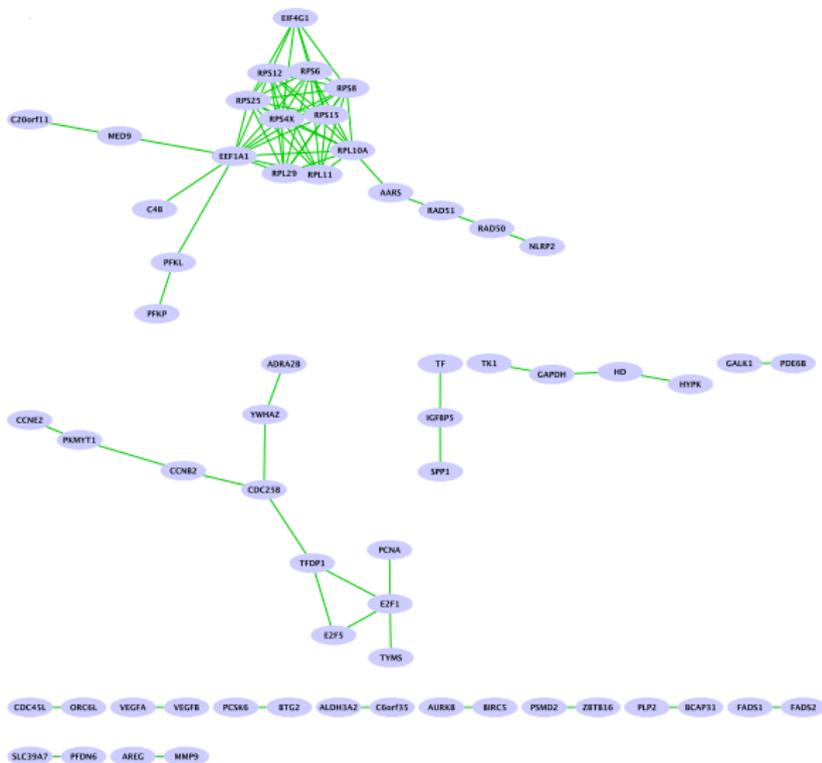


Lasso signature (accuracy 0.61)



Breast cancer prognosis, Jacob et al. (2009)

Graph Lasso signature (accuracy 0.64)

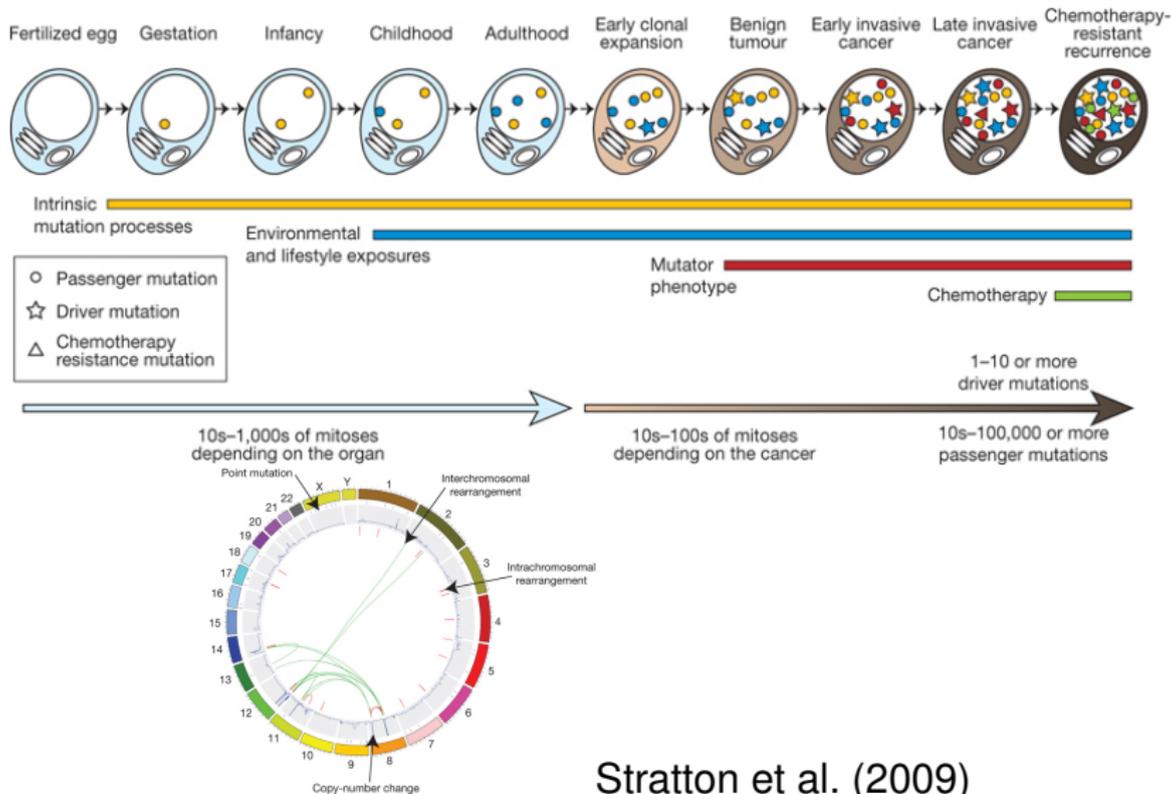


Breast cancer prognosis, Jacob et al. (2009)

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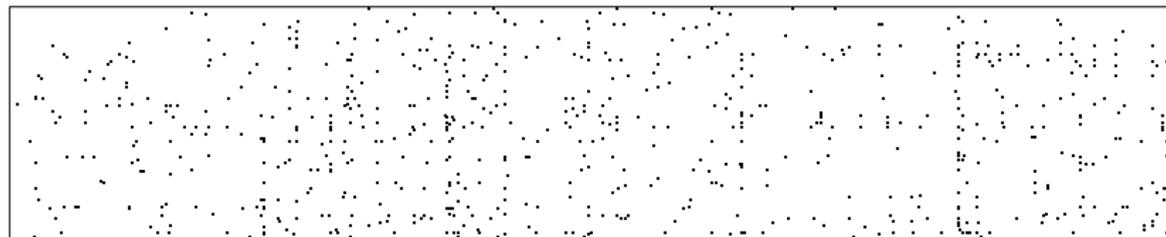
Somatic mutations in cancer



Stratton et al. (2009)

Large-scale efforts to collect somatic mutations

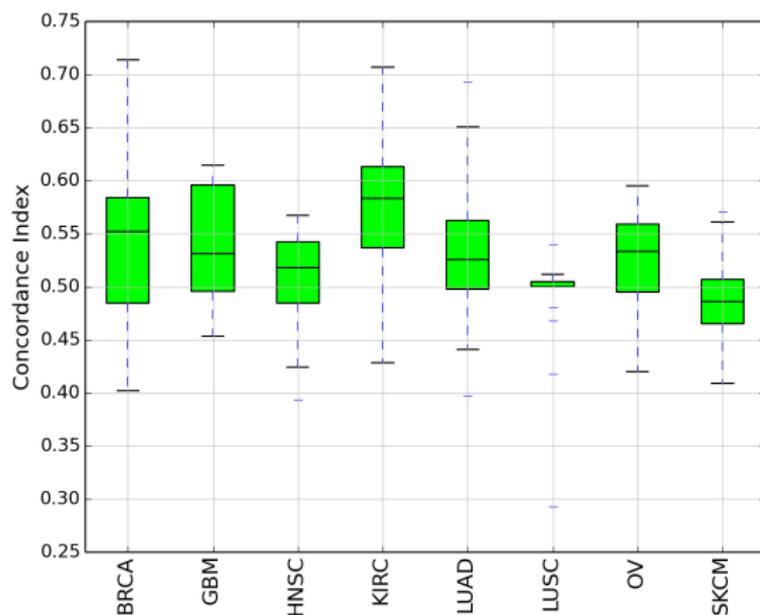
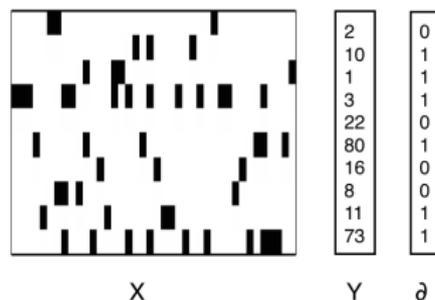
- **3,378 samples** with survival information from **8 cancer types**
- downloaded from the **TCGA / cBioPortal** portals.



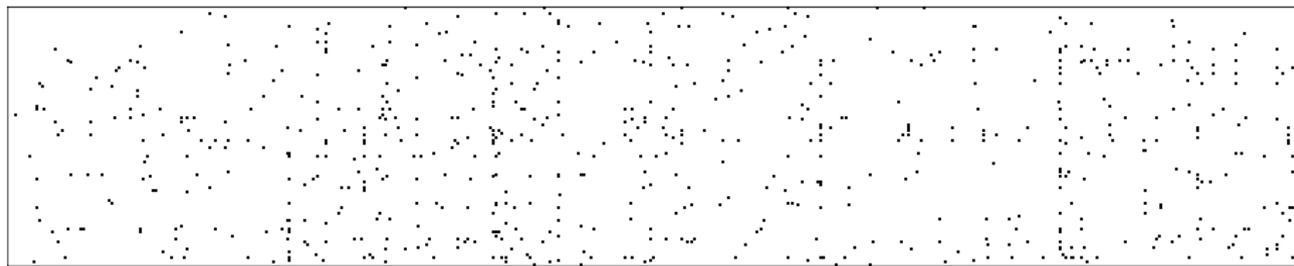
Cancer type	Patients	Genes
LUAD (Lung adenocarcinoma)	430	20 596
SKCM (Skin cutaneous melanoma)	307	17 463
GBM (Glioblastoma multiforme)	265	14 750
BRCA (Breast invasive carcinoma)	945	16 806
KIRC (Kidney renal clear cell carcinoma)	411	10 609
HNSC (Head and Neck squamous cell carcinoma)	388	17 022
LUSC (Lung squamous cell carcinoma)	169	13 590
OV (Ovarian serous cystadenocarcinoma)	363	10 195

Survival prediction from raw mutation profiles

- Each patient is a **binary vector**: each gene is mutated (1) or not (2)
- Silent mutations are removed
- Survival model estimated with sparse survival SVM
- Results on 5-fold cross-validation repeated 4 times



Changing the representation?



Can we replace

$x \in \{0, 1\}^p$ with p very large, very sparse

by a representation with more information shared between samples

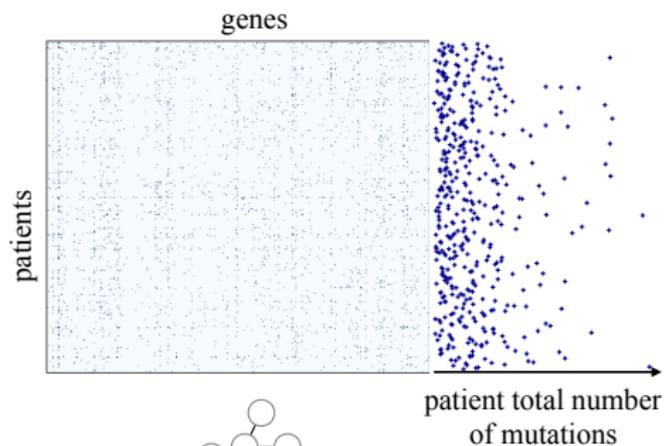
$\Phi(x) \in \mathcal{H}$?



NetNorm Overview (Le Morvan et al., 2016)

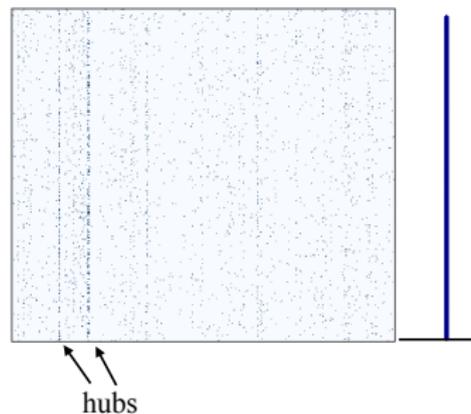
- **Modify** the binary vector $x \in \{0, 1\}^p$ of each patient by **adding or removing mutations**, using a **gene network** as prior knowledge
- After Netnorm, all patients $\Phi(x) \in \{0, 1\}^p$ have the **same number of (pseudo-)mutations**

Raw binary mutation matrix



Gene-gene interaction network

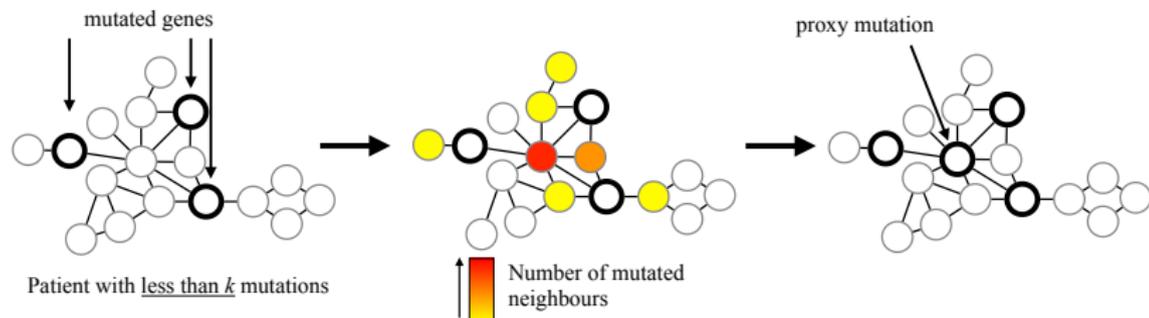
NetNorM binary mutation matrix



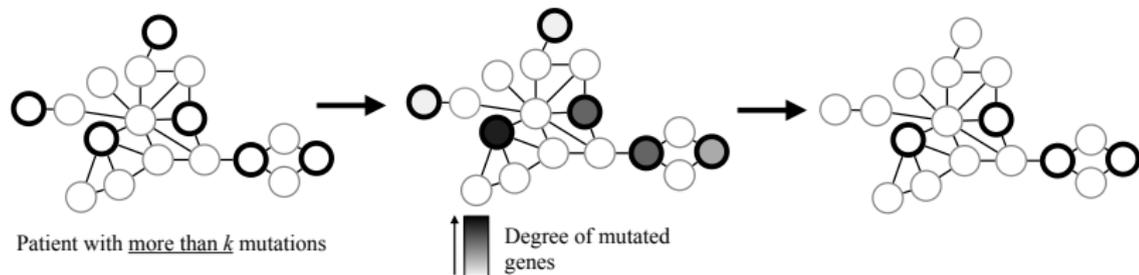
hubs

NetNorm detail ($k=4$)

- 1 **Add** mutations for patients with **few** (less than k) mutations



- 2 **Remove** mutations for patients for **many** (more than k) mutations



Network-based stratification of tumor mutations

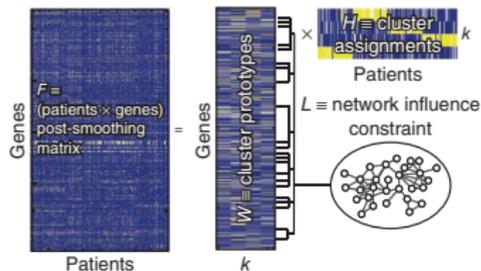
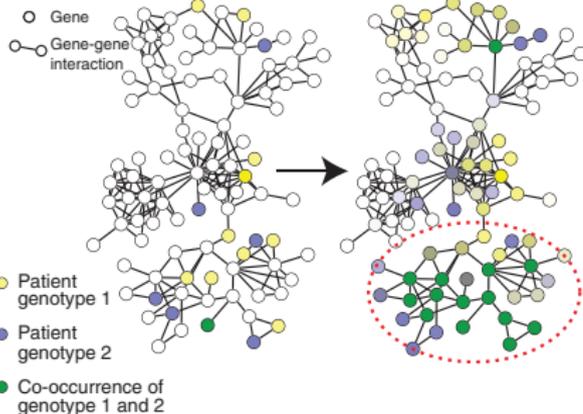
Matan Hofree¹, John P Shen², Hannah Carter², Andrew Gross³ & Trey Ideker¹⁻³

¹Department of Computer Science and Engineering, University of California, San Diego, La Jolla, California, USA. ²Department of Medicine, University of California, San Diego, La Jolla, California, USA. ³Department of Bioengineering, University of California, San Diego, La Jolla, California, USA. Correspondence should be addressed to T.I. (tideker@ucsd.edu).

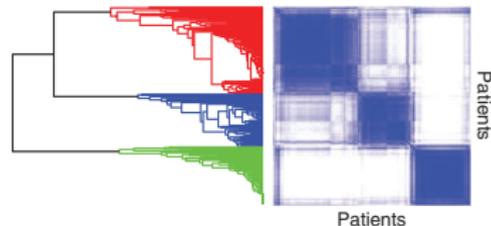
RECEIVED 14 FEBRUARY; ACCEPTED 12 AUGUST; PUBLISHED ONLINE 15 SEPTEMBER 2013; DOI:10.1038/NMETH.2651

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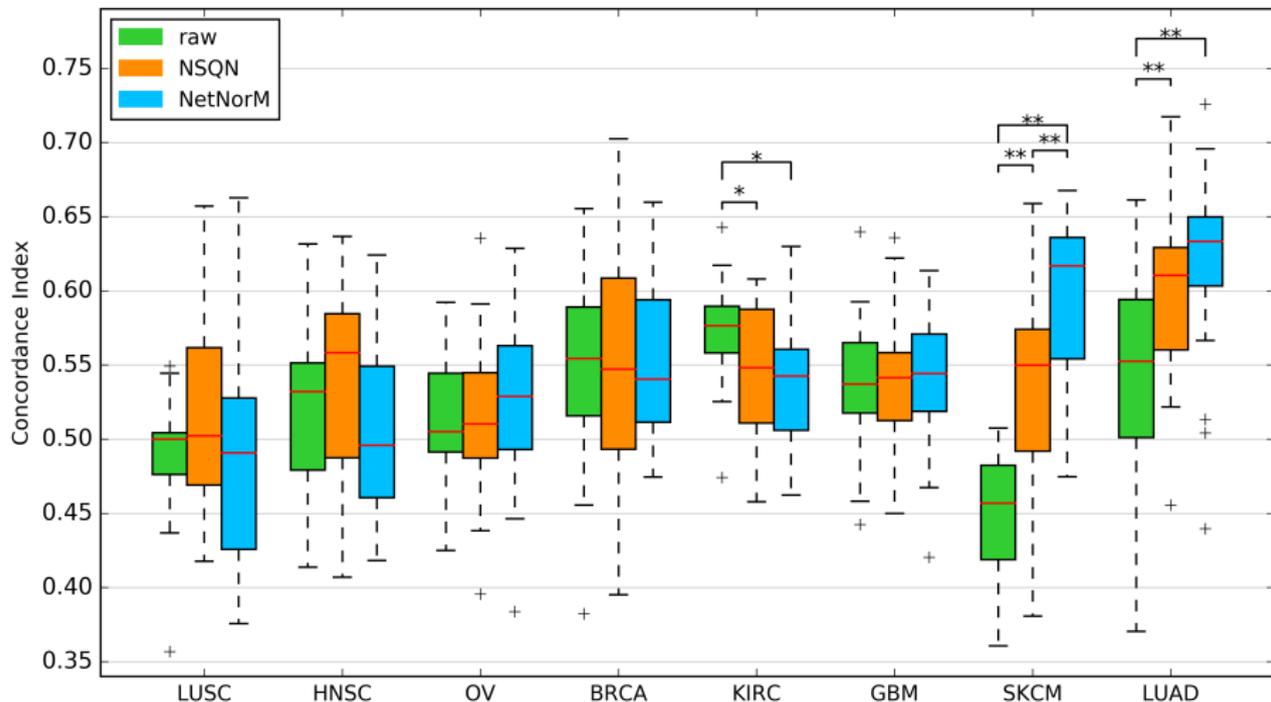
Network smoothing:



d Network-based stratification



Performance on survival prediction



Use Pathway Commons as gene network.

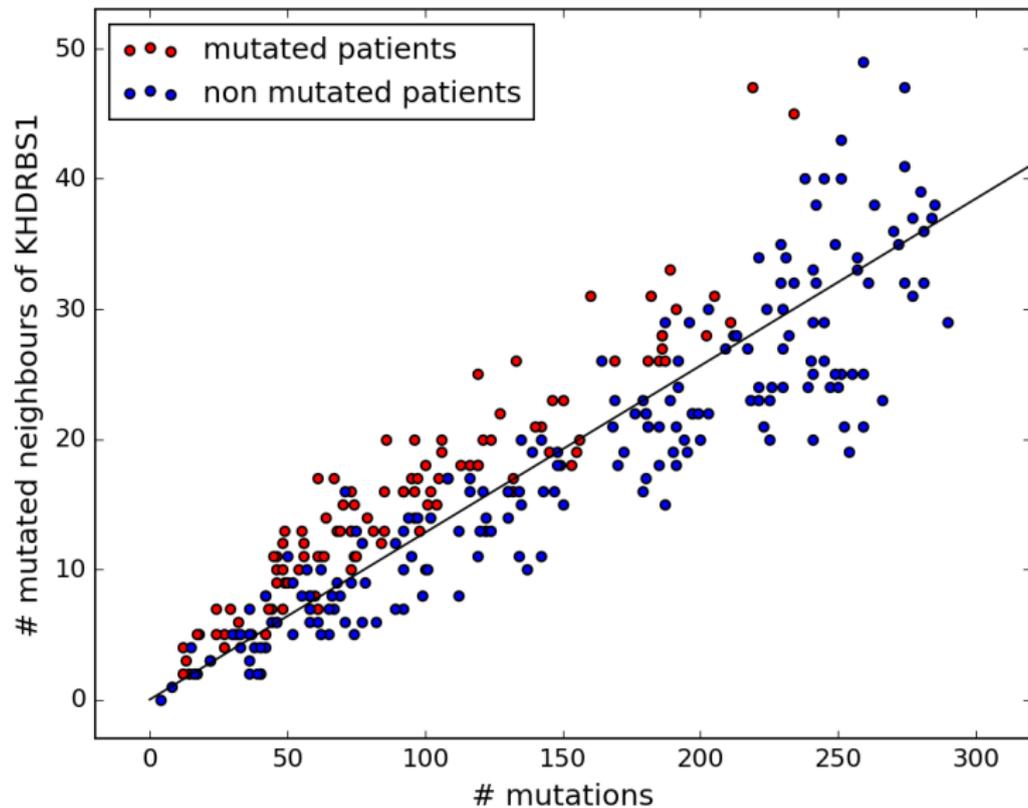
NSQN = Network Smoothing / Quantile Normalization (Hofree et al., 2013)

Selected genes represent "true" or "proxy" mutations

	freq	coef	m_{all}		$m_{<k_{med}}$		$m_{\geq k_{med}}$		Log-rank test (p-value)		Welsh t-test (p-value)	
			raw	NetNorM	raw	NetNorM	raw	NetNorM	raw	NetNorM	raw	NetNorM
TP53	19	-0.16	238	274	123	159	115	115	7.6×10^{-2}	9.4×10^{-2}	5.2×10^{-22}	1.2×10^{-13}
CRB1	18	-0.4	44	38	22	22	22	16	1.6×10^{-4}	1.4×10^{-6}	9.9×10^{-4}	6.9×10^{-2}
NOTCH4	17	-0.23	42	26	14	14	28	12	9.3×10^{-1}	3.3×10^{-2}	1.9×10^{-6}	2.6×10^{-1}
ANK2	17	0.1	90	90	33	33	57	57	1.2×10^{-2}	1.2×10^{-2}	6.3×10^{-10}	6.3×10^{-10}
RPS9	16	0.38	0	106	0	106	0	0	-	1.8×10^{-1}	-	4.2×10^{-47}
LAMA2	15	0.16	52	38	14	15	38	23	1.5×10^{-2}	2.3×10^{-2}	6.3×10^{-9}	2.6×10^{-3}
RYR2	14	0.07	165	161	70	70	95	91	1.4×10^{-2}	2.1×10^{-2}	6.7×10^{-19}	1×10^{-15}
IGF2BP2	14	-0.15	6	67	2	63	4	4	1.4×10^{-5}	3.6×10^{-3}	1×10^{-1}	6.8×10^{-7}
SMARCA5	14	-0.09	5	137	1	133	4	4	2.1×10^{-1}	5.3×10^{-3}	1.3×10^{-1}	1×10^{-27}
KHDRBS1	13	0.11	7	117	2	112	5	5	7.1×10^{-1}	9.7×10^{-1}	6.5×10^{-2}	1.3×10^{-18}
YWHAZ	13	-0.18	2	241	0	239	2	2	2.5×10^{-31}	6.1×10^{-4}	4.7×10^{-1}	4.4×10^{-37}
HRNR	13	-0.12	62	64	20	22	42	42	1.1×10^{-1}	1.1×10^{-1}	6×10^{-10}	2.9×10^{-9}
CSNK2A2	11	0.06	2	129	1	128	1	1	9×10^{-1}	8.8×10^{-1}	5.9×10^{-1}	4.2×10^{-27}
MED12L	11	0.04	27	27	8	8	19	19	5.5×10^{-2}	5.5×10^{-2}	1.7×10^{-4}	1.7×10^{-4}

- 14 genes are selected at least 50% of the time
- 6/14 are "proxy" genes (in blue)
 - big hubs in the network
 - get mutated by NetNorm in patients with few mutations \implies they encode the mutation rate
- 8/14 are "normal" prognostic genes

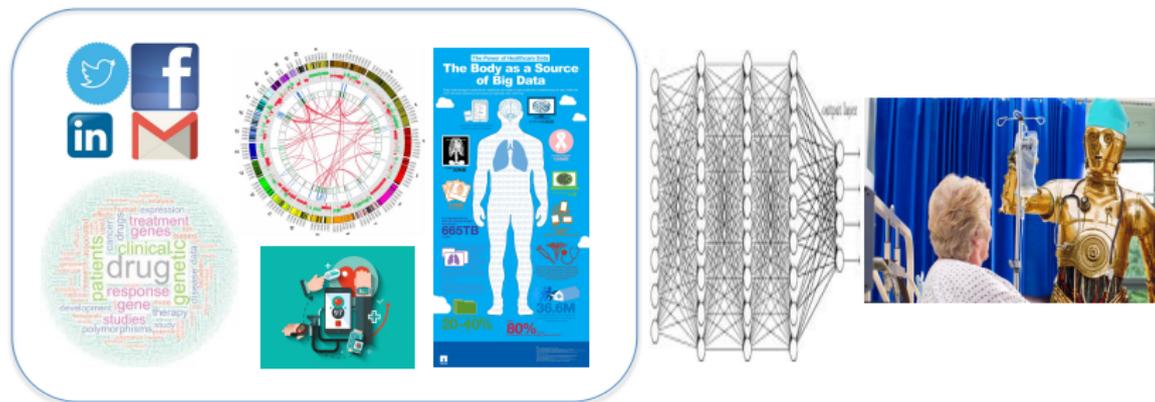
Proxy mutations encode local mutational burden



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Conclusion



- Many **new exciting problems** and **lots of data** in computational genomics and precision medicine
- $n \ll p$ problem requires dedicated methods
 - new **representations** $x \rightarrow \Phi(x)$
 - new **learning techniques** (structured sparsity, regularization, ...)

Thanks



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